

Hands on ParaGrandMC



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- Motivation for high-speed Monte Carlo
- Example studies with ParaGrandMC
- Parallelization strategy for Monte Carlo simulation method
- ParaGrandMC tutorial
- On hands exercises with ParaGrandMC





Sensory Alloy Concept

Creating a material with intrinsic sensory behavior*



- Improve early crack detection in metallic materials
- Improve vehicle reliability and safety
- Optimize structure and material performance (lower factor of safety)
- Decrease maintenance cost

Ferromagnetic Shape Memory Alloys (FSMA) as sensory material

High strain in damage zone causes phase transformation

- Acoustic emission (AE) that can be measured during flight
- Magnetic changes measurable using ground-based inspection equipment

System Preparation by MC Simulation



The simulations required the use of a substantial computational power and resources.

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Martensitic Transformation by MC



Lowering temperature initiates martensitic transformation at T < M_s

Crystal Structure

- BCC (austenite)
- HCP (twins)
- FCC (martensite)
- Undefined



The simulations required the use of a substantial computational power and resources.





γ/γ' interface in the Ni-Al system by capillary fluctuation method







Using the equilibrium power spectrum of the interface boundary fluctuations to extract the interface free energy.

Y Mishin

Figure 1. A typical snapshot of Monte Carlo simulations of γ and γ' phases at the temperature of 700 K. The simulation block is projected on the x-y plane showing only Al atoms. The red lines show the γ/γ' interfaces revealed by the visualization method applied in this work.







Initial system:

Perfectly flat interface: 512,000 atoms









Simulated for > 1,000,000 MCS













































Parallel Monte-Carlo Algorithm





- Apply spatial decomposition with link-cell technique
- Multiple atoms are selected in random

Then... how to deal with the sequential moves?







- Apply spatial decomposition with link-cell technique
- Multiple atoms are selected in random
- Group link-cells into sets of four in a checker board manner.

S. Plimpton et al., SANDIA report: SAND2009-6226, October (2009)



Parallel Monte-Carlo Algorithm





- Apply spatial decomposition with link-cell technique
- Multiple atoms are selected in random
- Group link-cells into sets of four in a checker board manner.
- Execute moves on atoms from the same set only.

This ensures that the trial atoms are far enough from each other, so that their moves are independent and can be executed simultaneously.







Switch between sets (1,.. 4) in a random fashion, until all chosen atoms are tried.







Switch between sets (1,.. 4) in a random fashion, until all chosen atoms are tried.







Switch between sets (1,.. 4) in a random fashion, until all chosen atoms are tried.







Parallelization in MC:

- Benefits from the spatial decomposition and the link-cell technique.
- Less efficient than MD with respect to multithread intra-node parallelization.

Development of ParaGrandMC Code



The code is in active development process – MPI+OpenMP+... (CUDA in the near future).

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Scalability comparison for different potential types

Distributed (MPI) + shared memory (OpenMP) parallelization on 16 MPI nodes with 1-16 cores/node



Scalability on a single node



ANN – Artificial Neural Network Machine Learning potential

TRF – Tersoff Potential 3-body potential (molecular crystals)

ADP – Angular Dependent Potential many-body anisotropic potential (rare earth metals)

EAM – Embedded Atom Method many-body isotropic potential (metal

alloys)

Speed up is limited for the functional potentials, but it is substantial for the ANN potential.





ParaGrandMC Tutorial: NASA/CR–2016-219202 http://www.sti.nasa.gov

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□ 1. Parallel Grand Canonical Monte Carlo (ParaGrandMC) Simulation Code Document ID: 20160007416 NTRS Full-Text: Click to View □ [PDF Size: 1.8 MB] Author: Yamakov, Vesselin I. Abstract: This report provides an overview of the Parallel Grand Canonical Monte Carlo (ParaGrandMC) Publication Year: 2016 Document Type: Technical Report Report/Patent Number: NASA/CR-2016-219202, NF1676L-24373 Date Acquired: Jun 10, 2016						



N = const

V = const

N- total number of particles

 $\Delta \Phi = \Delta E$

1. Canonical Monte Carlo:

constant volume (NVT):

Ensembles:

Displacement moves:











 $P = \begin{cases} 1 & , \Delta \Phi \le 0 \\ exp(-\Delta \Phi/k_BT), \Delta \Phi > 0 \end{cases} \qquad \begin{array}{l} \Delta \Phi \text{ - thermodynamic potential} \\ T = const \text{ - temperature} \end{cases}$

Ensembles:

- 1. Canonical Monte Carlo:
- **Displacement moves:**
- + volume change (strain):

2.



+ element change:



- N = constconstant volume (NVT): *V* = *const*
 - constant pressure (stress) (NPT):
- Semi-Grand Canonical MC: $\mu_{\alpha} = const$: constant volume (μ VT):

N- total number of particles

$$\Delta \Phi = \Delta E + \Delta \mu_{\alpha\beta} + \frac{3}{2} k_B T ln(m_{\alpha}/m_{\beta})$$

$$\sum_{\alpha} N_{\alpha}(\mu_{\alpha}) = const = N \qquad \Delta \mu_{\alpha\beta} = \mu_{\alpha} - \mu_{\beta}$$



N = const



Algorithm: Generate a random trial move and accept with a probability, *P*:

 $P = \begin{cases} 1 & , \Delta \Phi \leq 0 \\ exp(-\Delta \Phi/k_BT), \Delta \Phi > 0 \end{cases} \qquad \begin{array}{l} \Delta \Phi \text{ - thermodynamic potential} \\ T = const \text{ - temperature} \end{cases}$

Ensembles:

Displacement moves:

+ element change:

+ volume change (strain):

1. Canonical Monte Carlo:

-

- constant volume (NVT): V = const
- constant pressure (stress) (NPT):
- 2. Semi-Grand Canonical MC: $\mu_{\alpha} = const$:
 - constant volume (μ VT): P = const
 - constant pressure (stress) (μPT):

N- total number of particles

$$\Delta \Phi = \Delta E + \Delta \mu_{\alpha\beta} + \frac{3}{2} k_B T ln(m_{\alpha}/m_{\beta}) - N k_B T ln(V'/V)$$

$$\sum_{\alpha} N_{\alpha}(\mu_{\alpha}) = const = N \qquad \Delta \mu_{\alpha\beta} = \mu_{\alpha} - \mu_{\beta}$$

08/03/18





 $P = \begin{cases} 1 & , \Delta \Phi \leq 0 \\ exp(-\Delta \Phi/k_BT), \Delta \Phi > 0 \end{cases} \qquad \begin{array}{l} \Delta \Phi \text{ - thermodynamic potential} \\ T = const \text{ - temperature} \end{cases}$

Ensembles:

Displacement moves:

+ element change:

+ volume change (strain):

1. Canonical Monte Carlo:

-

2.

- onte Carlo: N = const
- constant volume (NVT): V = const
- constant pressure (stress) (NPT):

Semi-Grand Canonical MC: $\mu_{\alpha} = const$:

- constant volume (μ VT): P = const
- constant pressure (stress) (µPT):
- Feedback SGMC (cVT or cPT):

N- total number of particles

$$\Delta \Phi = \Delta E + \Delta \mu_{\alpha\beta} + \frac{3}{2} k_B T ln(m_{\alpha}/m_{\beta}) - N k_B T ln(V'/V)$$

$$\sum_{\alpha} N_{\alpha}(\mu_{\alpha}) = const = N \qquad \Delta \mu_{\alpha\beta} = \mu_{\alpha} - \mu_{\beta}$$

Concentration of element α , $c_{\alpha} \rightarrow c_{\alpha}^{0} = const$ $\mu_{\alpha}^{(n)} = \begin{cases} \mu_{\alpha}^{(n-1)} - a_{\alpha} \left(\frac{c_{\alpha}^{(n-1)} + c_{\alpha}^{(n-2)}}{2} - c_{\alpha}^{0} \right), for n \ge 2\\ \mu_{\alpha}^{(0)}, & for n < 2 \end{cases}$





 $P = \begin{cases} 1 & , \Delta \Phi \le 0 \\ exp(-\Delta \Phi/k_BT), \Delta \Phi > 0 \end{cases} \qquad \begin{array}{l} \Delta \Phi - \text{thermodynamic potential} \\ T = const - \text{temperature} \end{cases}$

Ensembles:

Displacement moves:

-

2.

- + volume change (strain):



+ element change:





- 1. Canonical Monte Carlo: N = const
 - constant volume (NVT): *V* = *const* constant pressure (stress) (NPT):
 - Semi-Grand Canonical MC: $\mu_{\alpha} = const$:
 - constant volume (μ VT): P = const
 - constant pressure (stress) (µPT):
 - Feedback SGMC (cVT or cPT):

- Variance-constrained SGMC:
 - B. Sadigh et al., Phys Rev B 85 (2012) 184203-1-11.

N- total number of particles

$$\Delta \Phi = \Delta E + \Delta \mu_{\alpha\beta} + \frac{3}{2} k_B T ln(m_{\alpha}/m_{\beta}) - N k_B T ln(V'/V)$$

$$\sum_{\alpha} N_{\alpha}(\mu_{\alpha}) = const = N \qquad \Delta \mu_{\alpha\beta} = \mu_{\alpha} - \mu_{\beta}$$

Concentration of element α , $c_{\alpha} \rightarrow c_{\alpha}^{0} = const$ $\mu_{\alpha}^{(n)} = \begin{cases} \mu_{\alpha}^{(n-1)} - a_{\alpha} \left(\frac{c_{\alpha}^{(n-1)} + c_{\alpha}^{(n-2)}}{2} - c_{\alpha}^{0} \right), \text{ for } n \ge 2\\ \mu_{\alpha}^{(0)}, & \text{ for } n < 2 \end{cases}$

$$\mu_{\alpha}^{(n)} = \begin{cases} \mu_{\alpha}^{(n-1)} - 2b_{\alpha} \frac{c_{\alpha}^{(n-1)} - c_{\alpha}^{(n-2)}}{2}, & for \ n \ge 2\\ \mu_{\alpha}^{(0)}, & for \ n < 2 \end{cases}$$







 $P = \begin{cases} 1 & , \Delta \Phi \le 0 \\ exp(-\Delta \Phi/k_BT), \Delta \Phi > 0 \end{cases} \qquad \begin{array}{l} \Delta \Phi - \text{thermodynamic potential} \\ T = const - \text{temperature} \end{cases}$

Ensembles:

Displacement moves:

- + volume change (strain):

-

2.

3.



+ element change:





- 1. Canonical Monte Carlo: N = constconstant volume (NVT): *V* = *const*
 - constant pressure (stress) (NPT):

Semi-Grand Canonical MC: $\mu_{\alpha} = const$:

- constant volume (μ VT): P = const
- constant pressure (stress) (µPT):
 - Feedback SGMC (cVT or cPT):

- Variance-constrained SGMC:
 - B. Sadigh et al., Phys Rev B 85 (2012) 184203-1-11.

Canonical MC with swap moves

N- total number of particles

$$\Delta \Phi = \Delta E + \Delta \mu_{\alpha\beta} + \frac{3}{2} k_B T ln(m_{\alpha}/m_{\beta}) - N k_B T ln(V'/V)$$

$$\sum_{\alpha} N_{\alpha}(\mu_{\alpha}) = const = N \qquad \Delta \mu_{\alpha\beta} = \mu_{\alpha} - \mu_{\beta}$$

Concentration of element α , $c_{\alpha} \rightarrow c_{\alpha}^{0} = const$ $\mu_{\alpha}^{(n)} = \begin{cases} \mu_{\alpha}^{(n-1)} - a_{\alpha} \left(\frac{c_{\alpha}^{(n-1)} + c_{\alpha}^{(n-2)}}{2} - c_{\alpha}^{0} \right), \text{ for } n \ge 2\\ \mu_{\alpha}^{(0)}, & \text{ for } n < 2 \end{cases}$

$$\mu_{\alpha}^{(n)} = \begin{cases} \mu_{\alpha}^{(n-1)} - 2b_{\alpha} \frac{c_{\alpha}^{(n-1)} - c_{\alpha}^{(n-2)}}{2}, & \text{for } n \ge 2\\ \mu_{\alpha}^{(0)}, & \text{for } n < 2 \end{cases}$$

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Molecular Dynamics regime to supplement MC simulations

- 1. Micro Canonical MD:
 - constant energy at fixed volume (NVE)
 5-th order Gear predictor-corrector integrator
- 2. Canonical MD:
 - constant temperature and volume (NVT)
 - constant temperature and pressure (stress) (NPT)
 Nose-Hoover thermostat + Parrinello-Rahman barostat

Allows seamless switch between MC and MD simulations





Structure File: structure.plt, or structure.lam – LAMMPS format

Example for plt – format (used in some old codes, e.g. "sold")

--- structure.plt ---

<pre># -0.1792446164E+02 -0.1788684653E+02 -0.1782515785E+02 # 0.1792446164E+02 0.1788684653E+02 0.1782515785E+02 # -0.1792446164E+02 -0.1788684653E+02 -0.1782515785E+02 # 0.1792446164E+02 0.1788684653E+02 0.1782515785E+02 # 2 4000 4000</pre>	! -h ₁₁ /2 -h ₂₂ /2 -h ₃₃ /2 initial ! h ₁₁ /2 h ₂₂ /2 h ₃₃ /2 initial ! -h ₁₁ /2 -h ₂₂ /2 -h ₃₃ /2 current ! h ₁₁ /2 h ₂₂ /2 h ₃₃ /2 current ! n/a N_atoms, N_buf, N_free	$ \begin{aligned} x_i &= h_{11} s_{xi} + h_{12} s_{yi} + h_{13} s_{zi} \\ y_i &= h_{22} s_{yi} + h_{23} s_{zi} \\ z_i &= h_{33} s_{zi} \end{aligned} $
# 0.6/248840E+01 1 1 1 1 # -1 -1 -1	! n/a ! n/a	h h h $-$ 0 in plt format
# 0 0	! n/a	$n_{12}, n_{13}, n_{23} = 0$ in pit format.
# -0.4430826192E+01 922.6	! Pot.energy/atom, T of the system	Use LAMIMPS (.lam) file format
224 -0.1789335455E+02 0.1597144817E+01 0.1494689416E+01	2 2 ! id X Y Z type constraint	
226 -0.1619578319E+02 0.1830532545E+01 0.3288215770E+01	1 0 ! .	
230 -0.1617572658E+02 0.1722213549E+01 0.7033719156E+01	1 0 ! .	
•		
3682 0.1612777159E+02 -0.8918761584E+01 -0.1782246887E+02	2 1 0	
1	! 0: no velocities; 1: with velociti	es
224 0.1405660198E+01 0.000000000E+00 0.1132724982E+01	! id v_x v_y v_z (Å/ps)	
226 0.9420957345E+01 -0.2580232213E+01 0.1855807313E+01		
230 -0.1426233611E+01 0.4245608319E+01 0.1019702603E+01		
3682 -0.1731818246E+01 0.2910471448E+01 -0.7523290612E+00	0	
1.0 1.0	! default numbers for end of file.	





Potential File: pot.dat (Inherited from "sold")

Examples:

NiAl EAM potential from NIST repository: www.ctcms.nist.gov/potentials/

--- pot.dat ---

2 – number of chemical spe	ecies in the system
'Ni' 58.71 ! chemica	l symbol and atomic mass
'Al' 26.982	-
0 - regular EAM alloy pote	ential 🚽
'./NiAl-2004/pni.dat'	! pair Ni–Ni potential
'./NiAl-2004/pnial.dat'	! pair Ni-Al potential
'./NiAl-2004/pal.dat'	! pair Al-Al potential
'./NiAl-2004/fni.dat'	! Ni electron density
'./NiAl-2004/fal.dat'	! Al electron density
'./NiAl-2004/F_ni.dat'	! Ni embedded function
'./NiAl-2004/F al.dat'	! Al embedded function

NiAl EAM potential in LAMMPS format:

```
2 lammps - number of chemical species in the system
'Ni' 58.71  ! chemical symbol and atomic mass
'Al' 26.982
0 - regular EAM alloy potential
'./NiAl-2004/NiAl2004.eam.alloy' ! path and file name
```

Currently supported potential formats:

- 0: EAM alloy potential
- 1: ADP Angular Dependent Pot.
- 2: MEAM (in progress)
- 3: Tersoff (conventional: Tersoff_1 in LAMMPS)
- 4: Tersoff-modified:

see T.Kumagai et al., Comp. MAt. Sci (2007) 456

- 5: EAM/fs Finnis-Sinclair EAM
- 6: BOP Bond Order Potential (Y. Mishin format)
- 100: ANN Straight Arfitificial Neural Netwrok
- 106: ANN-BOP Physically guided ANN (see James talk)
- .. more to come





Command File: pgmc.com

A script text file with commands and parameters to control the simulation

Example:

pgmc.com		ΛΙ
ini: 2 600.0 0.05 0.0005	! Initialization with <mc_rank> <temp> <dr> <dh h=""></dh></dr></temp></mc_rank>	AI
3	! Number of elements	
Al	! First element (as defined in the pot.dat file)	
Со	! Second element	
Ni	! Third element	
'Filename'	! Output filename (up to 64 symbols)	
input: plt	! Input structure file format (plt, or lam for LAMMPS input)	
output: lam	! Output structure file format (LAMMPS format in this case)	
time: 10000	! Start time (MCS or MDS)	
# MC specific parameters for	ollow: ! Comment line, not executed	
comp: 0.29 0.36 0.35	! Chemical composition (sum = 1.0)	
mue: 0.0 -0.43 0.28	! Chemical potentials for each element (one must be 0)	
alpha: 0.0 0.01 0.01	! Multiplier coefficients to each mue (ensemble types 3-6)	
mc: 1 1000 10 300.0 2 3 0	! MC run with parameters	
# MD specific parameters	follow:	
md stone 2.0	I MD time stop (fa), default value 1.0	
linu_step: 2.0	! MD time step (is); default value 1.0	
diss: 1.0	Heat dissipation coefficient for the Nose-Hoover thermos	stat
wmass: 16.0	! Effective wall mass for Parrinello-Rahmann const. stress	
wdamp: 25.0	! Effective wall damping for Parrinello-Rahmann const. str	ess
md: 1 1000 10 300.0 1 3 0) ! MD run with parameters	
end:	! end of the simulation (no commands are executed after t	hat)
	`	,

All commands are given in Appendix A of the Users Manual





Structure File: filename.########.plt, or filename. ########.lam – LAMMPS format

Format: same as the input structure file (can be used directly as an input file). ######### - 8 digits number indicating the number of MCS (or fs in MD regime) e.g. NiAl_model.00123456.lam

Stress File (optional): filename.#########.stress

Example:

atom id, atom type, σ_{xx} , σ_{yy} , σ_{zz} , σ_{xy} , σ_{xz} , σ_{yz} , E_p 236 1

 σ_{ij} - stress components in GPa E_p - potential energy in eV.





Data File: filename.########.dat

Reported data is specified by command "measure:" in the pgmc.com file

Example:

--- pgmc.com ---

'Ni85Al15 N4k'

! Output filename

measure: hii Ti! Measured parametersmc: 1 30 10 300.0 3 3 0! nruns nsteps rep_step T ens irig, isvmd: 1 30 10 300.0 0 1 0! nruns nsteps rep_step T ens irig, isvend:

Output:

••

--- Ni85Al15_N4k.0000000.dat ---

Run	step	<pre>Time(MCS/fs)</pre>	Ek	Ep	Etot	Т(К)	h(1 , 1)	h(2,2)	h(3 , 3)	T(Al)	T(Ni)
	0	0.00	0.02851095	-4.53168118	-4.50317023	220.57	3.5287	3.5333	3.5296	138.14	664.87
	10	10.00	0.03877800	-4.54034854	-4.50157054	300.00	3.5283	3.5346	3.5302	300.00	300.00
	20	20.00	0.03877800	-4.55407302	-4.51529502	300.00	3.5299	3.5344	3.5322	300.00	300.00
	30	30.00	0.03877800	-4.57035424	-4.53157625	300.00	3.5310	3.5349	3.5351	300.00	300.00
	10	40.00	0.04200614	-4.57356222	-4.53155608	324.97	3.5310	3.5349	3.5351	322.48	307.39
	20	50.00	0.04640474	-4.57796082	-4.53155608	359.00	3.5310	3.5349	3.5351	351.25	323.41
	30	60.00	0.04683165	-4.57838769	-4.53155604	362.31	3.5310	3.5349	3.5351	345.83	341.65

Suitable for plotting





Visualization File: filename.#########.imd

IMD type format used by OVITO (Open Visualization Tool) program

Visualized data is specified by command "ovito:" in the pgmc.com file



#X

#Y

#Z

#F





What is beneficial in PGMC?

- Massively parallel MC/MD code for large systems (~ 10⁶-10⁷ atoms)
- Implements regimes not always found in other MC codes (Semi-Grand Canonical with Feed-Back or Variation Constrained algorithms)
- Supports ANN and Physically Inspired NN potentials the newest generation of machine learning potentials
- Under active development to utilize the most advanced HPC hardware
- It is free upon request (subject to NASA requirements)

https://software.nasa.gov/search/software/ParagrandMC