

PyFit-FF Introduction

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Acknowledgments

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*** NASA

Talk Outline

- **Background**

- Machine learning, numerical optimization, regression
- Neural networks
- PyTorch and automatic differentiation

- **PYFIT-FF**

- Machine learning interatomic potentials
 - ANN, PINN,
- Functionality and overview

- **Demonstration**

- Installations process
- Closer look at the code
 - Input and output files
 - README+Manual+Code details
- Fitting example
- Q & A

BACKGROUND

Machine learning

Supervised Learning
Algorithms learn a functional mapping between *pairs of known inputs and output*



Regression
curve fitting to continuous numeric variables

Classifications
training models to identify known categories present in the data

Unsupervised Learning
Algorithms find connections inherent in the data. This data has no known a priori structure *i.e. no known mapping between inputs and outputs*



Clustering

Dimensionality reduction

Reinforcement Learning
Algorithms learn desired behaviors based on rules and some definition of desirable and undesirable outcomes



The goal is to learn to choose decisions that produces the optimal outcomes

Algorithms



Neural networks as function interpolants

- Gaussian processes
- linear regression

- Logistic regression
- Classification trees (ensembles)
- Deep learning (neural networks)
- support vector machines (SVM)
- Naive Bayes algorithm

- K means
- K medians
- expectation maximization (EM)
- hierarchical clusters
- TSNE, PCA

- Feature selection: keep only important features
- Feature extraction: Find new features are created

- Examples: Robot navigation, real time decision making
- Markov decision process
 - set of nodes with penalties on each path
- Guided output based on programmed reinforcement and punishments

Numerical optimization

Numerical solvers:

$$f(x) = 0$$

Numerical Optimizers:

$$\min(f(x)) \rightarrow \frac{df(x)}{dx} = 0$$

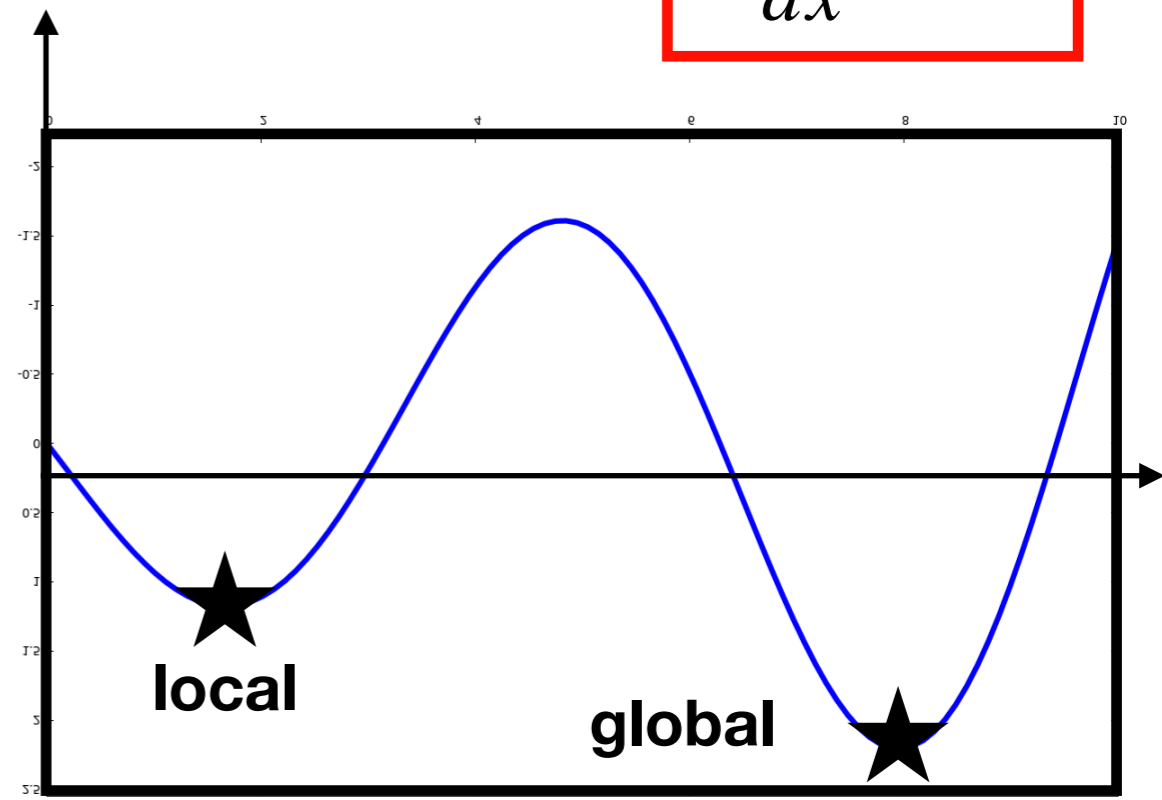
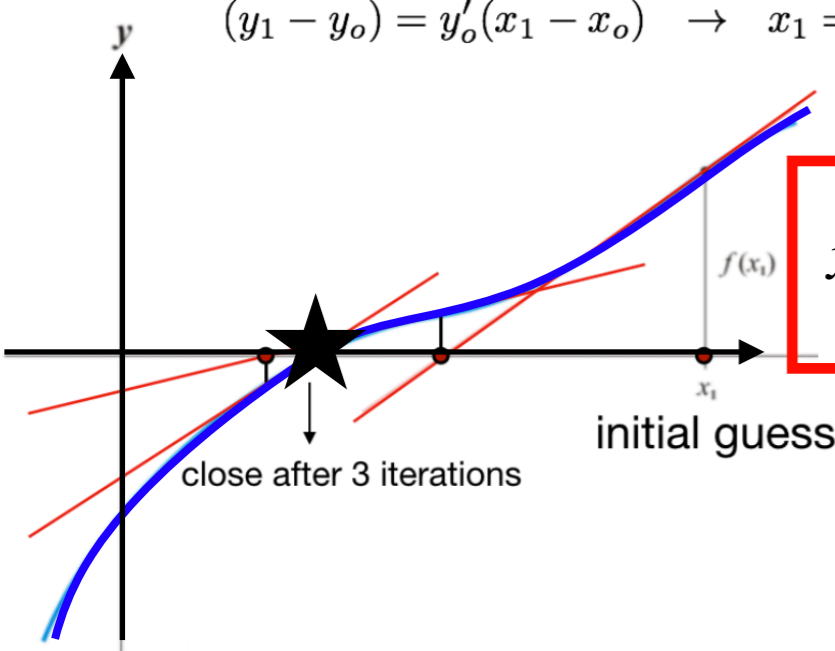
Point slope equation of tangent line

$$(y_1 - y_0) = y'_0(x_1 - x_0) \rightarrow x_1 = x_0 - \frac{y_0}{y'_0} \text{ (for } y_1 = 0)$$

Find intercept

Newton's method

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$



Gradient based Optimizers:

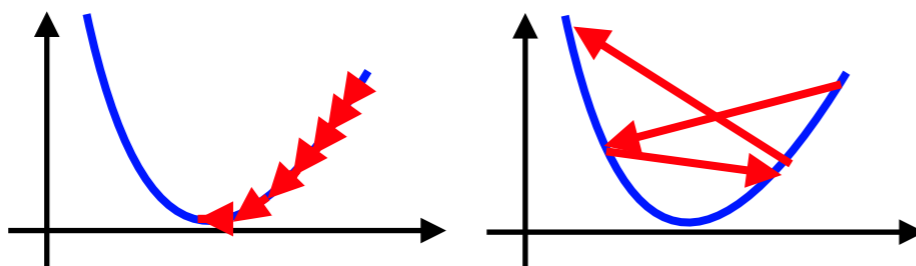
- Newton's method
- Secant method
- Gradient decent
- Davidon-Fletcher-Powell (DFP)
- Conjugate Gradient Method
- ★ Broyden-Fletcher-Goldfarb-Shanno (BFGS)

Newton's method $x_{n+1} = x_n - \frac{f'(x_n)}{f''(x_n)}$

Gradient decent $\rightarrow x_{n+1} = x_n - \lambda f'(x_n)$

Multivariable case: $\mathbf{x}_{n+1} = \mathbf{x}_n - \lambda \nabla F(\mathbf{x}_n)$

step size ("learning rate")



Regression

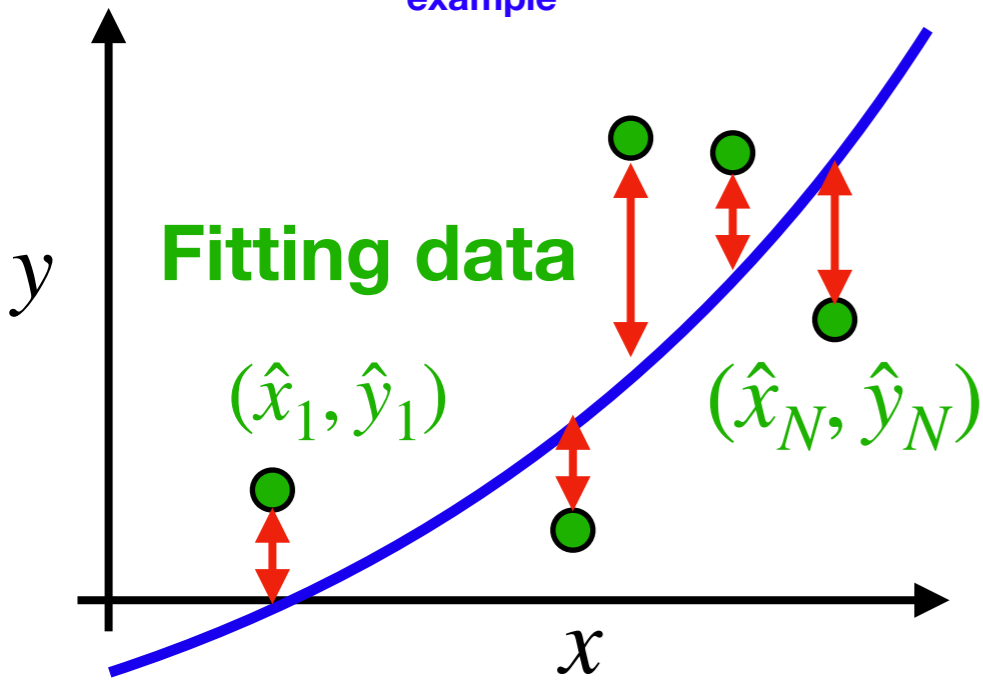
Fitting Model (interpolant)

$$y = F(x, \mathbf{w}) \rightarrow y = w_0 + w_1x + w_2x^2$$

example

Fitting Parameters

$$\mathbf{w} = (w_0, w_1, w_2)$$



Error Metric (objective)

RMSE:

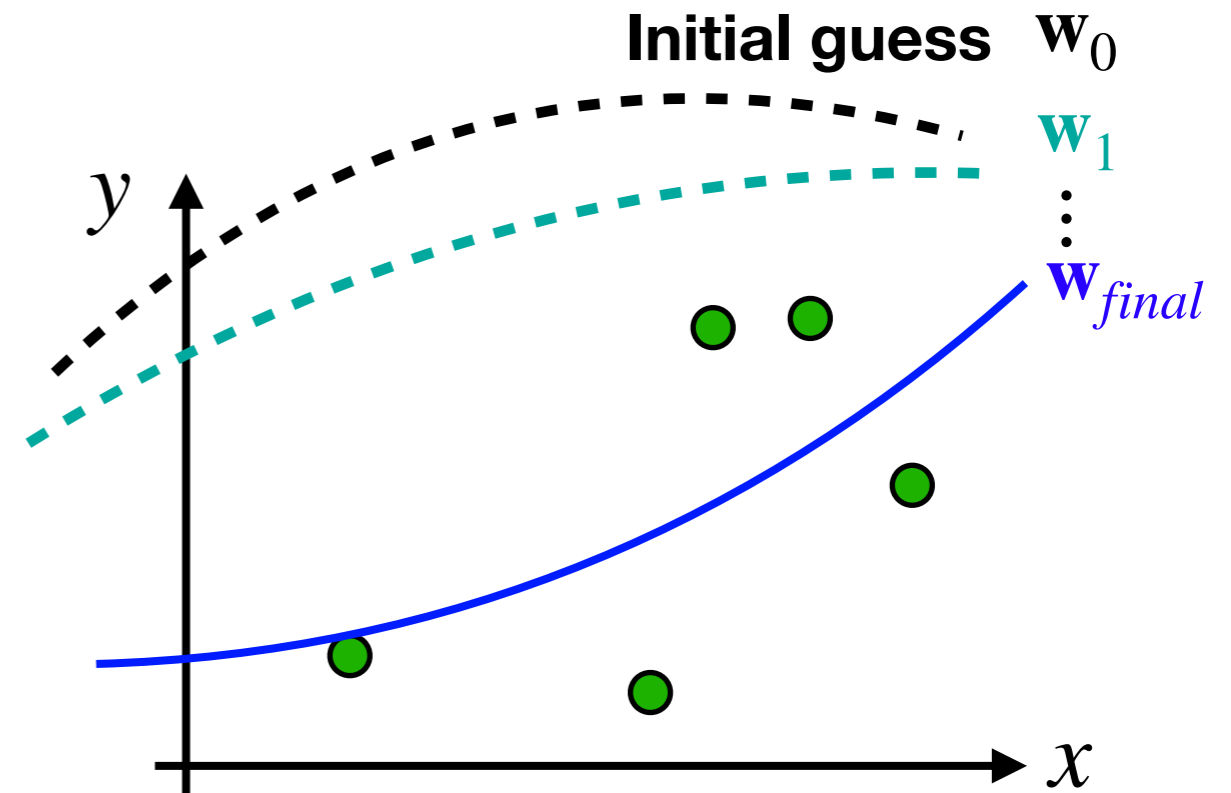
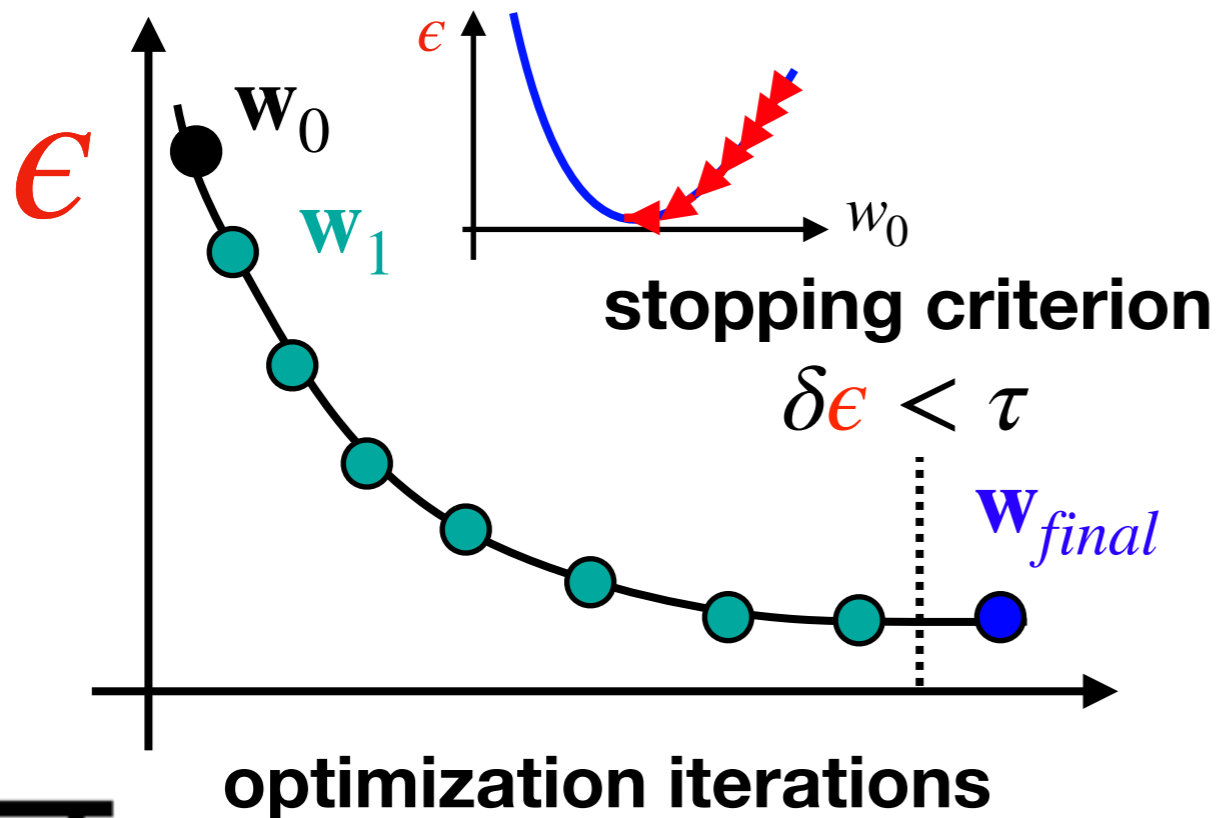
$$\epsilon(\mathbf{w}) = \sum_i \left(\frac{(y_i - \hat{y}_i)^2}{N} \right)^{\frac{1}{2}}$$

$$y_i = F(\hat{x}_i | \mathbf{w})$$

Alternatives: MAE, MSE, MEDIAN AE, ETC

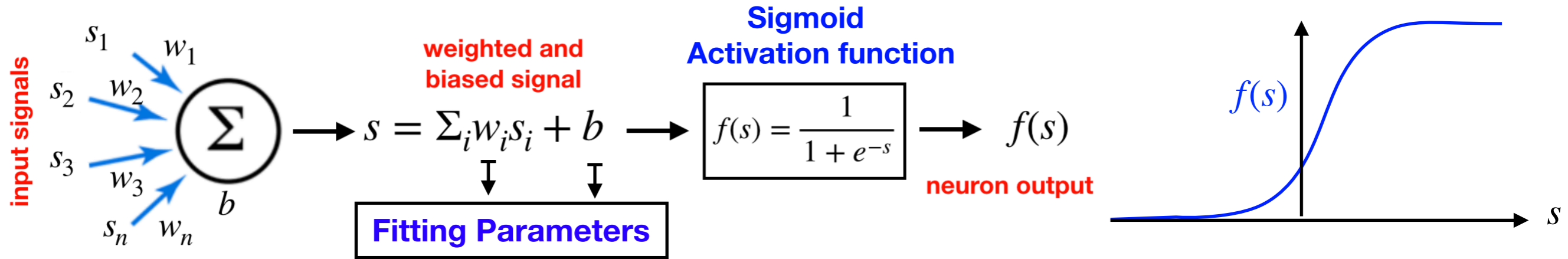
Numerical optimization

minimize error via fitting parameters



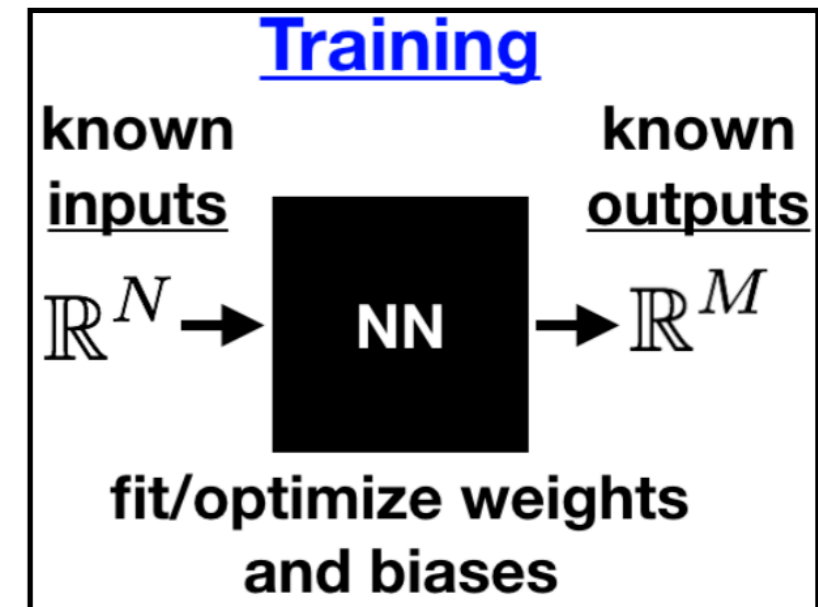
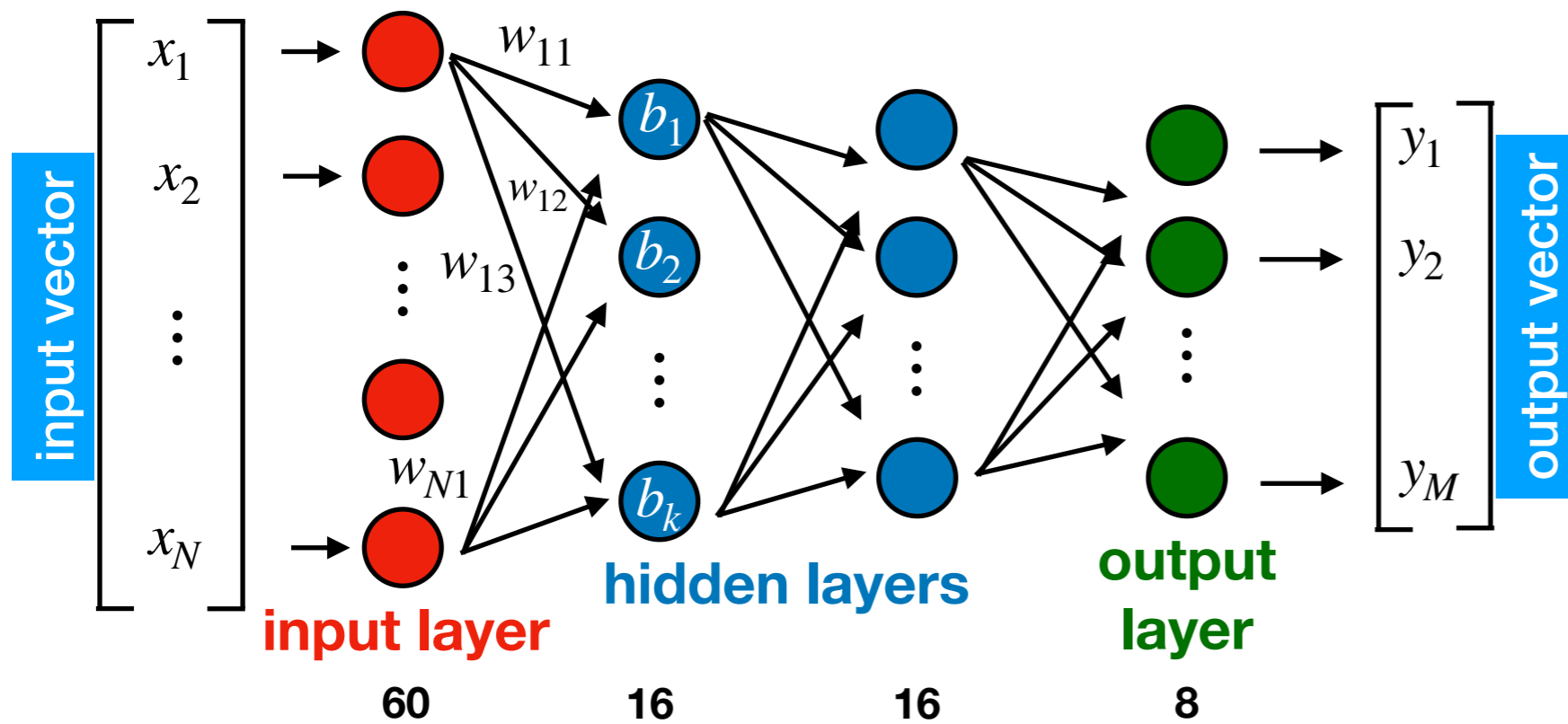
Neural networks: General idea

Artificial neuron



Artificial neural network

NN=generalized high dimensional regression function



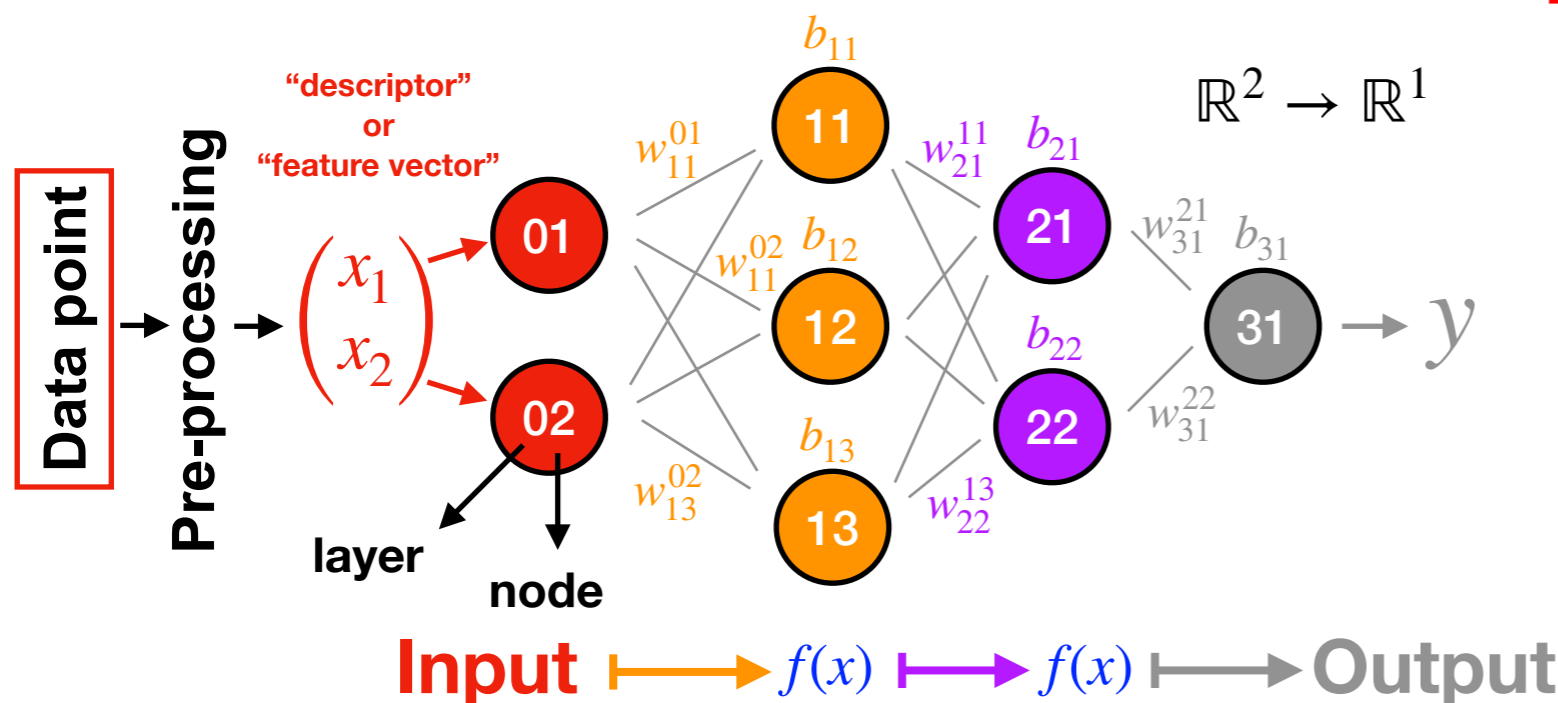
Neural network model

$$y = NN(\mathbf{x}, \mathbf{w})$$

Quadratic model

$$y = F(x, \mathbf{w}) = w_0 + w_1x + w_2x^2$$

Neural networks: Implementation-1



NN architecture: 2-3-2-1

Number of fitting parameters:

$$N_{fit} = (3 \times 2 + 3) + (2 \times 3 + 2) + (2 \times 1 + 1) = 20$$

Activation function:

$$f(x) = \frac{1}{1 + e^x}$$

stack

- w_{11}^{01}
- w_{12}^{01}
- w_{13}^{01}
- w_{11}^{02}
- w_{12}^{02}
- w_{13}^{02}
- b_{11}
- b_{12}
- b_{13}
- w_{21}^{11}
- w_{22}^{11}
- w_{21}^{12}
- w_{22}^{12}
- w_{21}^{13}
- w_{22}^{13}
- b_{21}
- b_{22}
- w_{31}^{21}
- w_{31}^{22}
- b_{31}

Hidden layer-1 output $\xrightarrow{f(x)}$
$$\begin{pmatrix} O_{11} \\ O_{12} \\ O_{13} \end{pmatrix} = f \left(\begin{pmatrix} w_{11}^{01} & w_{11}^{02} \\ w_{12}^{01} & w_{12}^{02} \\ w_{13}^{01} & w_{13}^{02} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \begin{pmatrix} b_{11} \\ b_{12} \\ b_{13} \end{pmatrix} \right)$$

apply activation function component wise

Hidden layer-2 output $\xrightarrow{f(x)}$
$$\begin{pmatrix} O_{21} \\ O_{22} \end{pmatrix} = f \left(\begin{pmatrix} w_{21}^{11} & w_{21}^{12} & w_{21}^{13} \\ w_{22}^{11} & w_{22}^{12} & w_{22}^{13} \end{pmatrix} \begin{pmatrix} O_{11} \\ O_{12} \\ O_{13} \end{pmatrix} + \begin{pmatrix} b_{21} \\ b_{22} \end{pmatrix} \right)$$

Neural network output $\xrightarrow{f(x)}$
$$y = (O_{31}) = (w_{31}^{21} \quad w_{31}^{22}) \begin{pmatrix} O_{21} \\ O_{22} \end{pmatrix} + (b_{31})$$

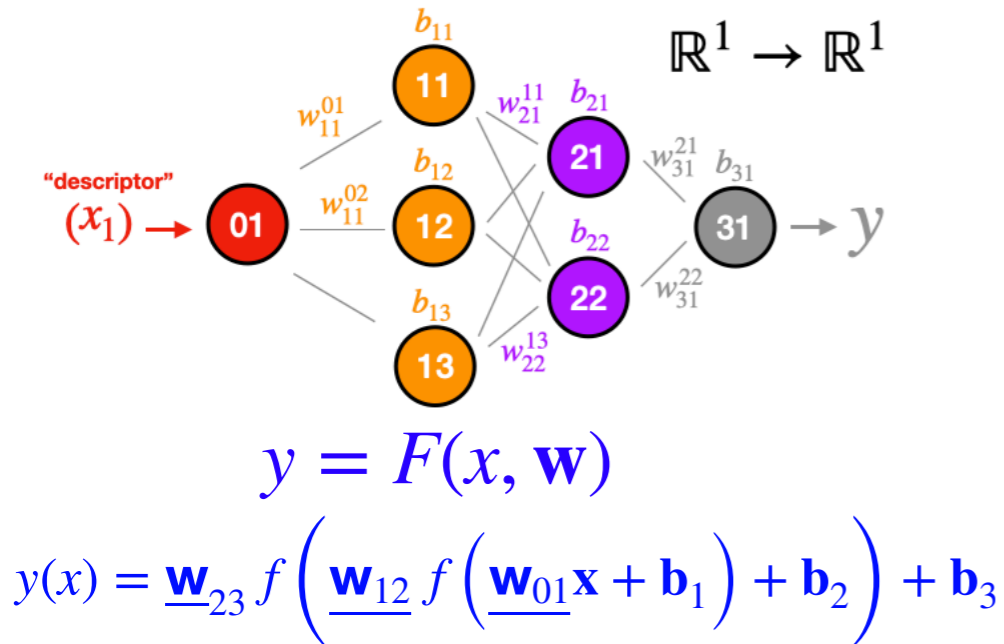
Don't apply activation function on output layer

Matrix form:

$$y = \underline{\mathbf{w}}_{23} f \left(\underline{\mathbf{w}}_{12} f \left(\underline{\mathbf{w}}_{01} \mathbf{x} + \mathbf{b}_1 \right) + \mathbf{b}_2 \right) + \mathbf{b}_3$$

Neural networks: Training

Neural network fitting model



Fitting parameters

- $$\mathbf{w} = \begin{pmatrix} w_{11}^{01} \\ w_{12}^{01} \\ w_{13}^{01} \\ b_{11} \\ b_{12} \\ b_{13} \\ w_{21}^{11} \\ w_{22}^{11} \\ w_{21}^{12} \\ w_{22}^{12} \\ w_{21}^{13} \\ w_{22}^{13} \\ b_{21} \\ b_{22} \\ w_{31}^{21} \\ w_{31}^{22} \\ b_{33} \end{pmatrix}$$

Numerical optimization to find best fit

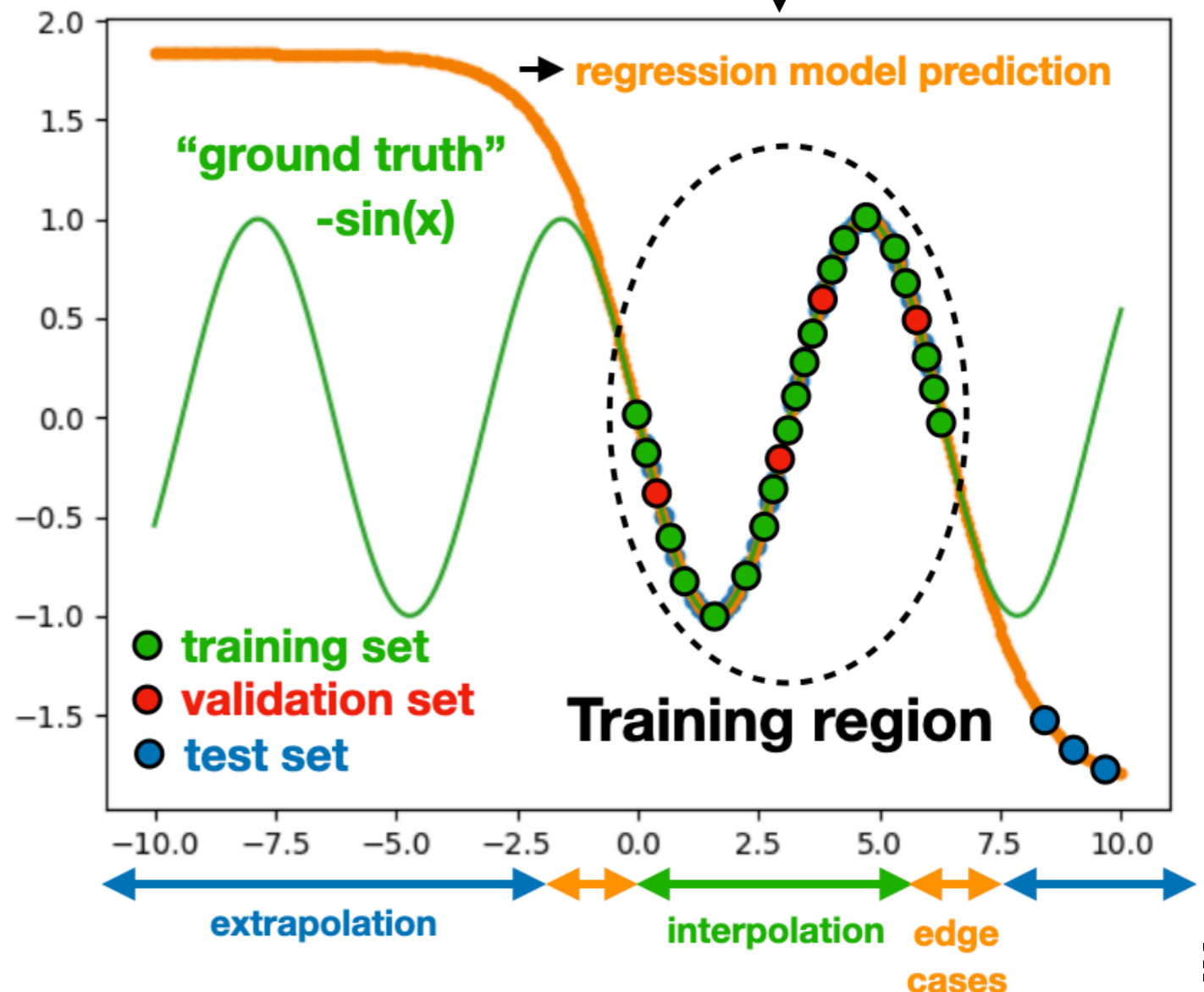
Sine function fitting model

$$y = F(x, \mathbf{w})$$

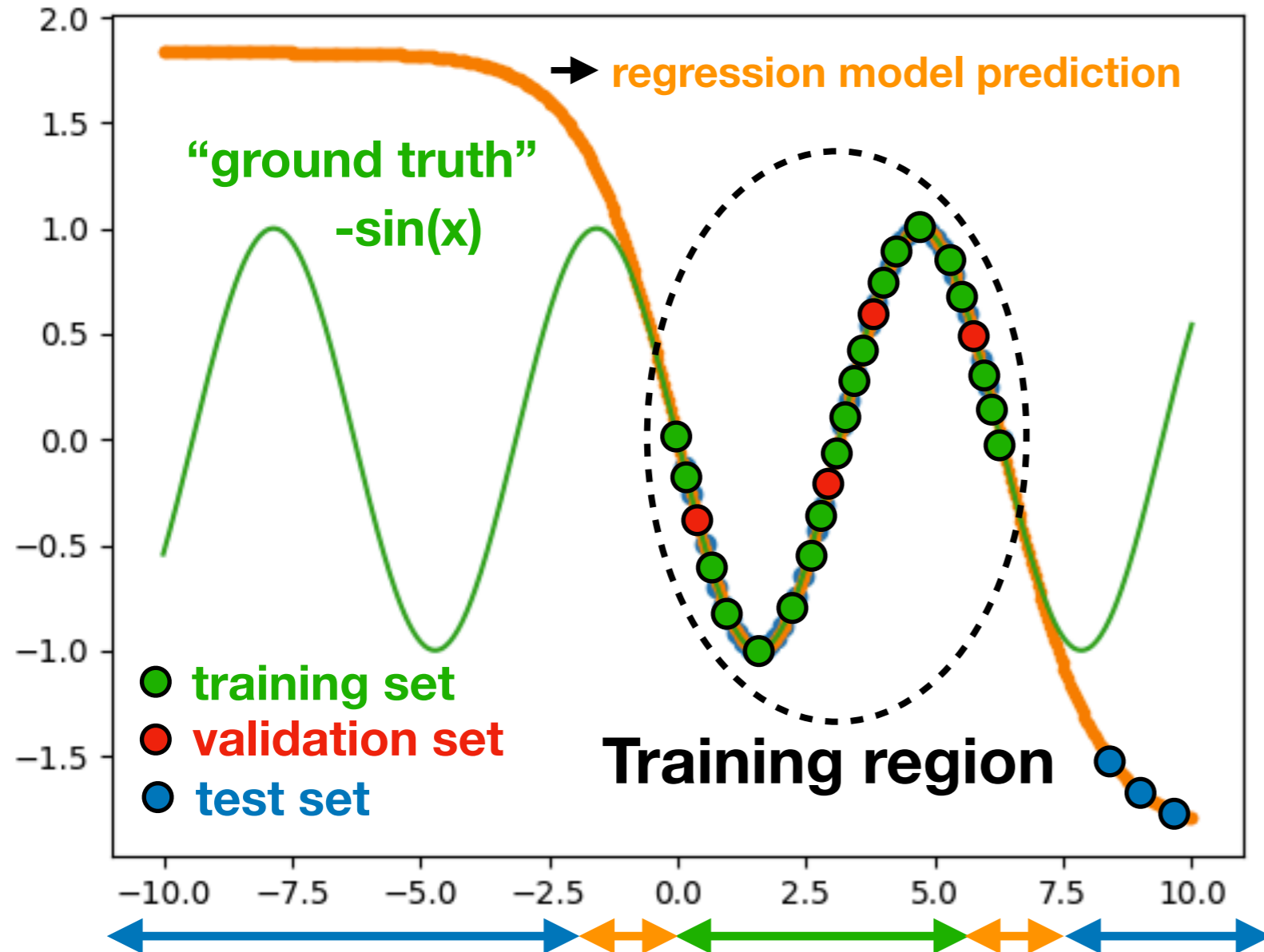
$$y(x) = A \sin(\omega(x - x_0)) + C$$

Fitting parameters $\mathbf{w} = (A, \omega, x_0, C)$

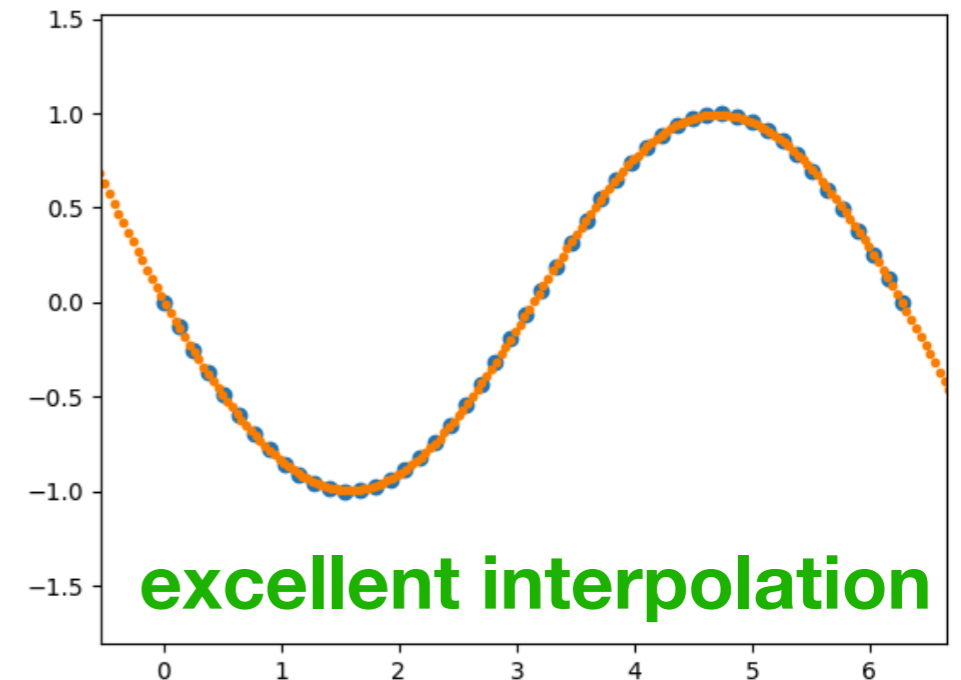
Numerical optimization to find best fit



Neural networks: General concerns



Train NN to reproduce provided data



Validation data (~10-20% of the data)
 -untrained but similar to training data
 -tests interpolation
 -used to monitor under/over fitting

Test data

-untrained but different from train and validation data
 -tests extrapolation or “transferability”

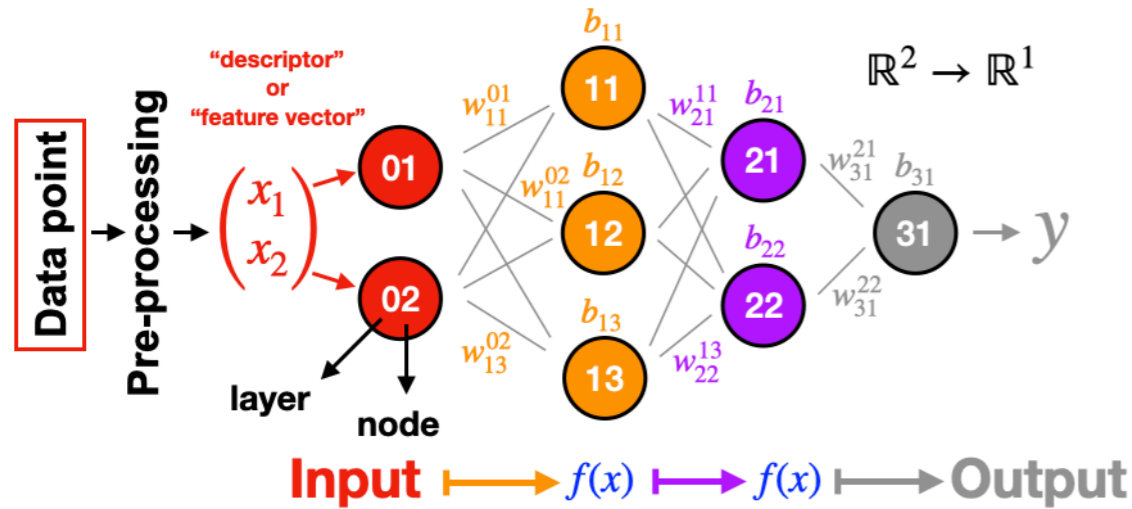
under-fitting
 model complexity is too low

optimal
 correct level of model complexity

over-fitting
 model complexity is too high

Neural networks: Implementation-2

Batch implementation (multiple inputs \rightarrow multiple outputs)



Identical neural network!!

$$\begin{pmatrix} x_1 & x_2 \end{pmatrix} \rightarrow \text{Input vector-1}$$

$$\begin{pmatrix} \tilde{x}_1 & \tilde{x}_2 \end{pmatrix} \rightarrow \text{Input vector-2}$$

Hidden layer-1:

Single input:
$$\begin{pmatrix} O_{11} \\ O_{12} \\ O_{13} \end{pmatrix} = f \left(\begin{pmatrix} w_{11}^{01} & w_{11}^{02} \\ w_{12}^{01} & w_{12}^{02} \\ w_{13}^{01} & w_{13}^{02} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \begin{pmatrix} b_{11} \\ b_{12} \\ b_{13} \end{pmatrix} \right) \quad f(\underline{\mathbf{w}}_{01} \mathbf{x} + \mathbf{b}_1)$$

Multiple inputs:

$$\begin{pmatrix} O_{11} & O_{12} & O_{13} \\ \tilde{O}_{11} & \tilde{O}_{12} & \tilde{O}_{13} \end{pmatrix} = f \left(\begin{pmatrix} x_1 & x_2 \\ \tilde{x}_1 & \tilde{x}_2 \end{pmatrix} \begin{pmatrix} w_{11}^{01} & w_{12}^{01} & w_{13}^{01} \\ w_{11}^{02} & w_{12}^{02} & w_{13}^{02} \end{pmatrix} + \begin{pmatrix} b_{11} & b_{12} & b_{13} \\ b_{11} & b_{12} & b_{13} \end{pmatrix} \right) \quad f(\mathbf{x} \underline{\mathbf{w}}_{01}^T + \mathbf{b}_1)$$

Single input:

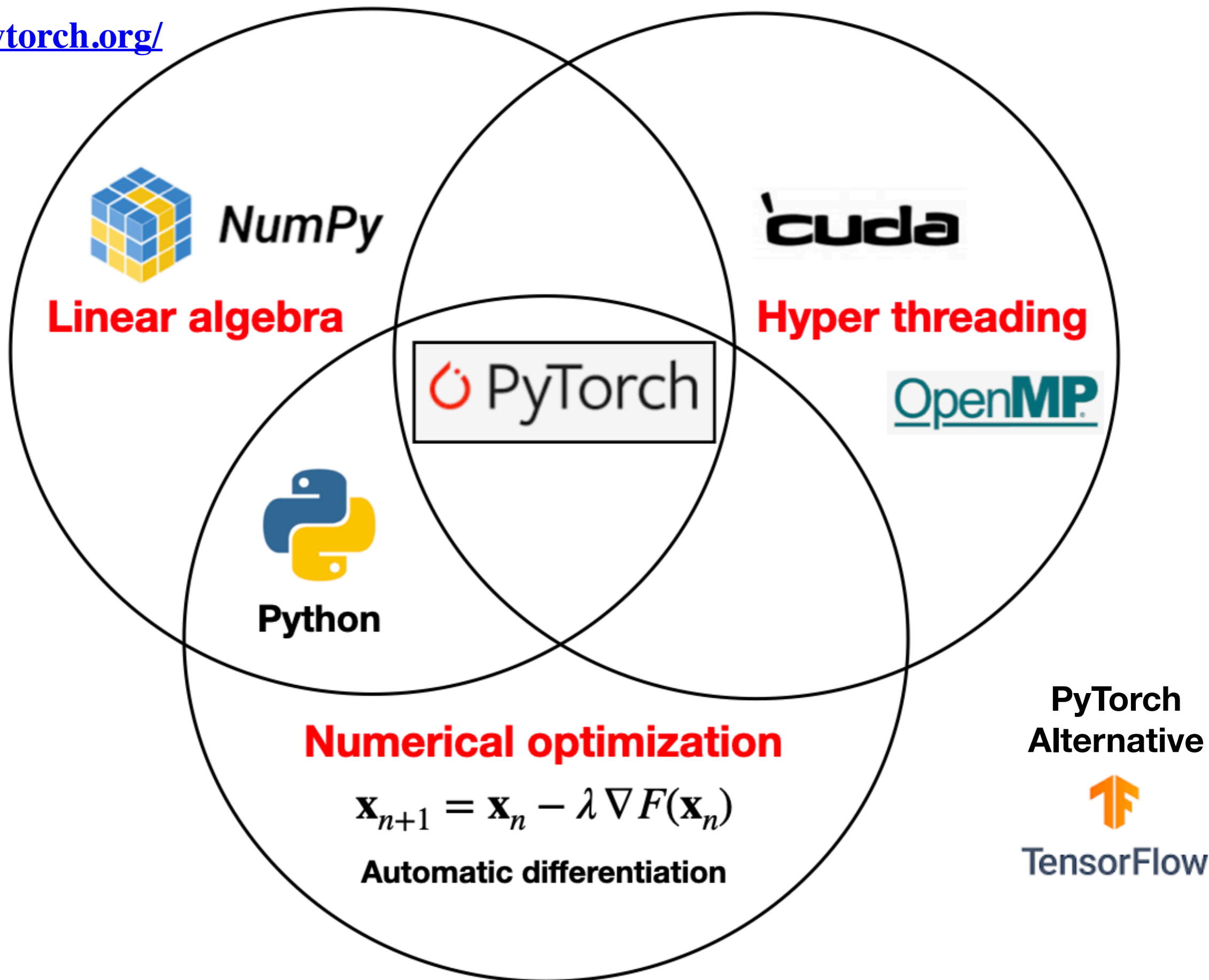
$$y = \underline{\mathbf{w}}_{23} f \left(\underline{\mathbf{w}}_{12} f \left(\underline{\mathbf{w}}_{01} \mathbf{x} + \mathbf{b}_1 \right) + \mathbf{b}_2 \right) + \mathbf{b}_3$$

multiple inputs:

$$\begin{pmatrix} y \\ \tilde{y} \end{pmatrix} = f \left(f \left(\mathbf{x} \underline{\mathbf{w}}_{01}^T + \mathbf{b}_1 \right) \underline{\mathbf{w}}_{12}^T + \mathbf{b}_2 \right) \underline{\mathbf{w}}_{23}^T + \mathbf{b}_3$$

PyTorch Overview

<https://pytorch.org/>



Automatic differentiation

Automatic differentiation

https://en.wikipedia.org/wiki/Automatic_differentiation

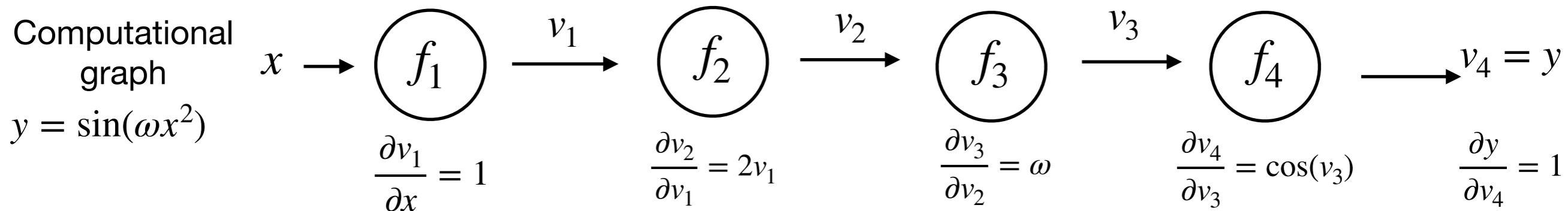
- Track operations
- Form computational graph
- Differentiate via chain rule
 - Forward mode
 - Reverse mode

AUTOGRAD 

```
>>> x = torch.randn(5, 5) # requires_grad=False by default
>>> y = torch.randn(5, 5) # requires_grad=False by default
>>> z = torch.randn((5, 5), requires_grad=True)
>>> a = x + y
>>> a.requires_grad
False
>>> b = a + z
>>> b.requires_grad
True
```

<https://pytorch.org/docs/stable/notes/autograd.html>

Toy Example: inside $v_1 = f_1(x) = x$ $v_2 = f_2(v_1) = v_1^2$ $v_3 = f_3(v_2) = \omega v_2$ $v_4 = f_4(v_3) = \sin(v_3)$ out



Function evaluation

$$y = f_4(f_3(f_2(f_1(x))))$$

$$v_1 = f_1(x) = x$$

$$v_2 = f_2(v_1) = v_1^2$$

$$v_3 = f_3(v_2) = \omega v_2$$

$$v_4 = f_4(v_3) = \sin(v_3) = y$$

Chain rule

$$\frac{dy}{dx} = \frac{dy}{dv_4} \frac{dv_4}{dv_3} \frac{dv_3}{dv_2} \frac{dv_2}{dv_1} \frac{dv_1}{dx}$$

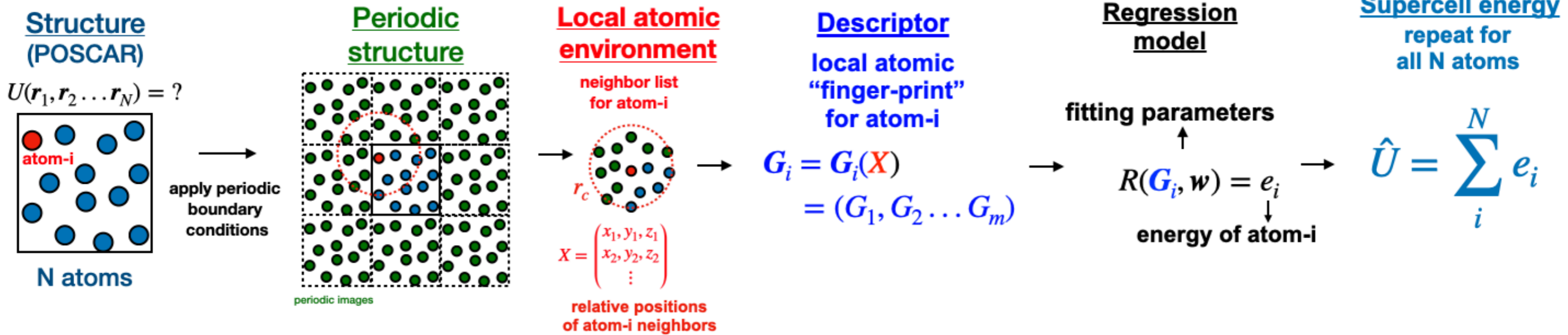
$$\frac{dy}{dx} = 2\omega x \cos(\omega x^2) \rightarrow y'(2)$$

evaluate numerically

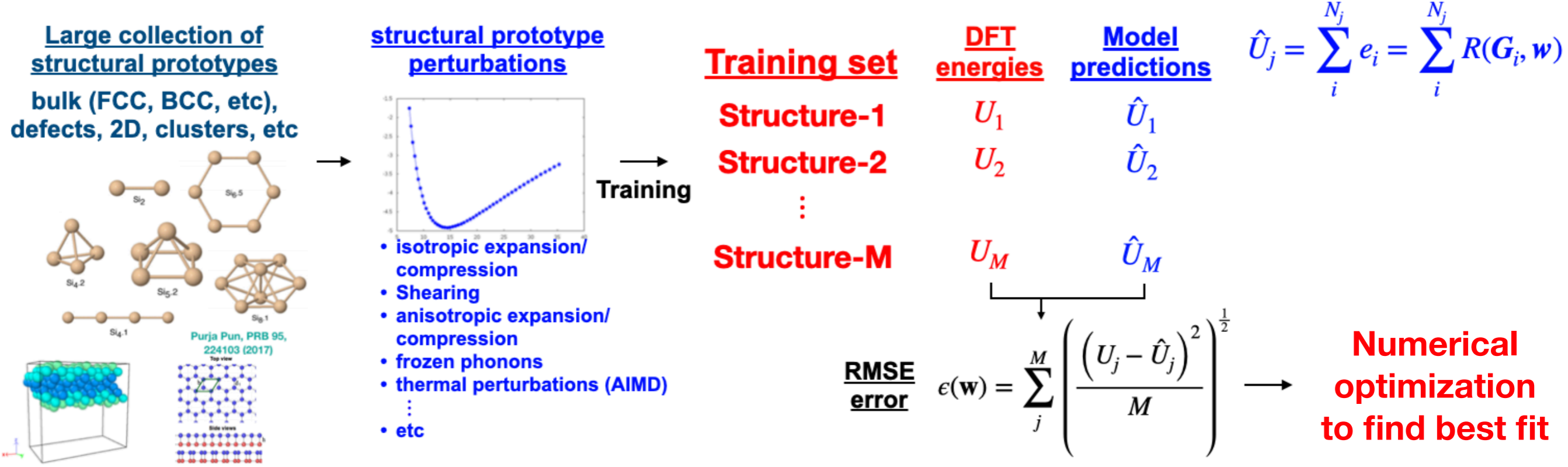
PYFIT-FF

Machine learning potentials: General

Model:



Training:

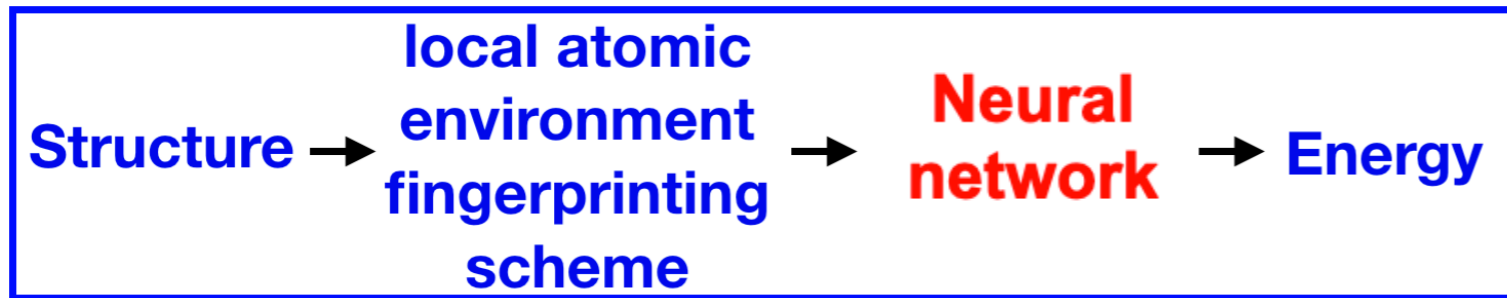


Potential types

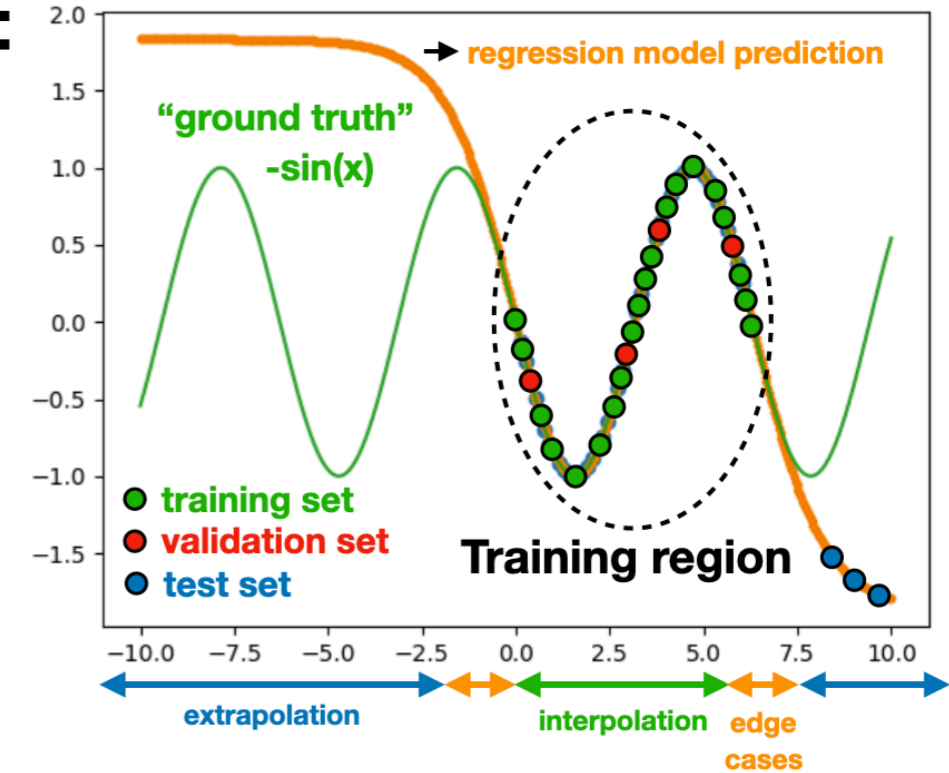
Traditional potential model



ANN potential model

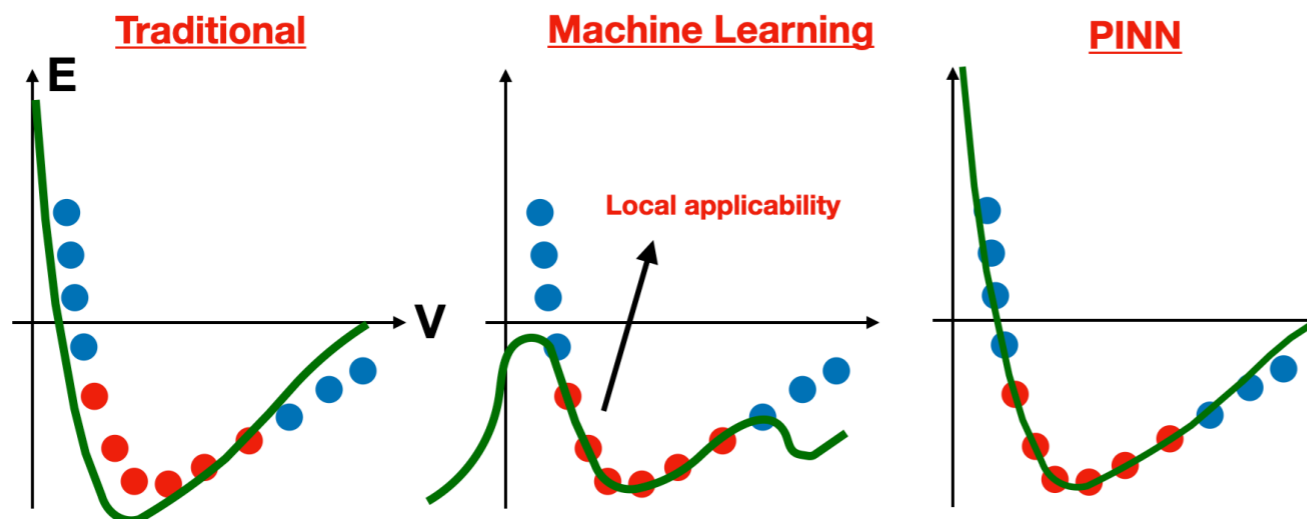
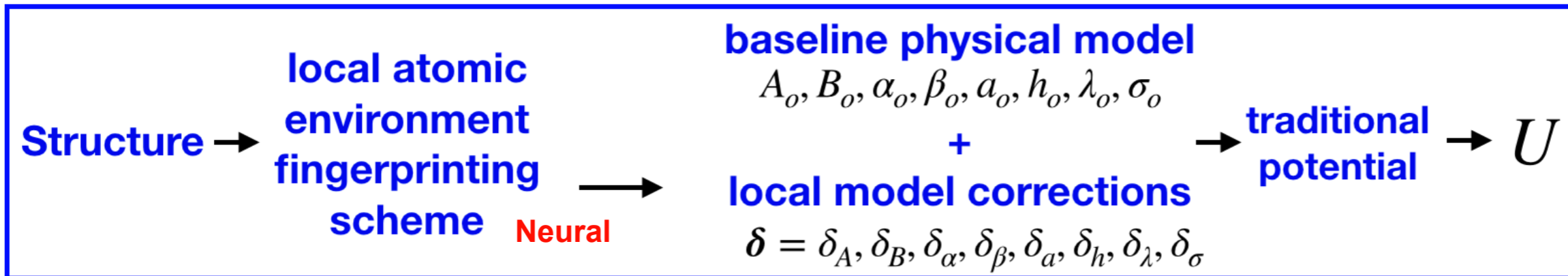


Analogy:



PINN potential model

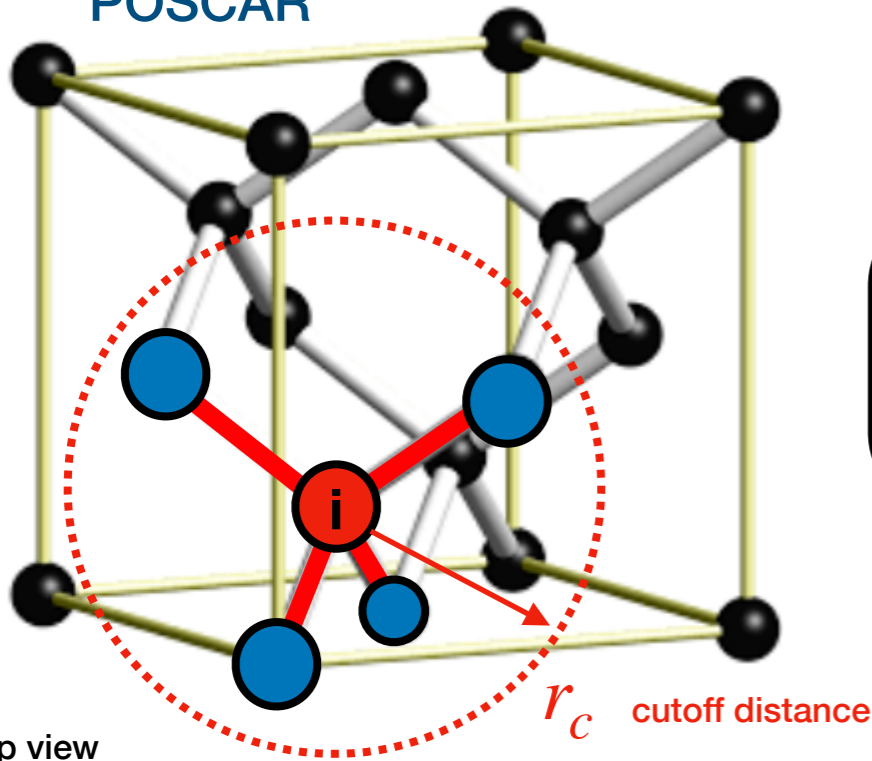
Physically informed artificial neural networks for atomistic modeling of materials
GPP Pun, R Batra, R Ramprasad, Y Mishin - Nature communications, 2019



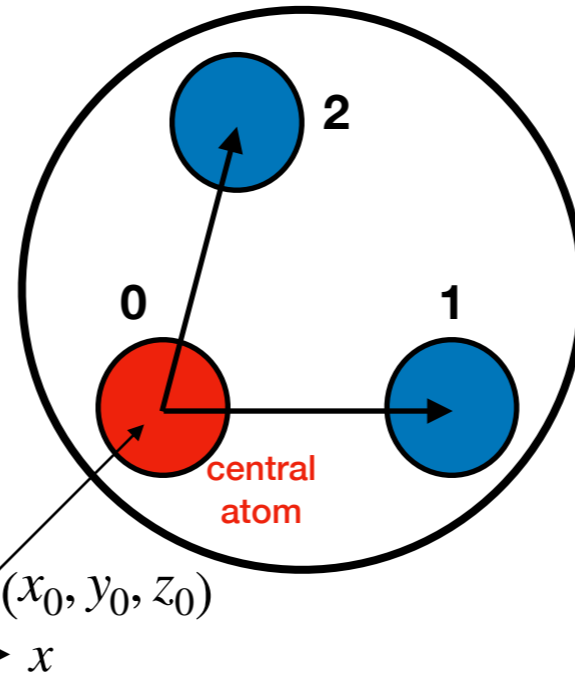
Atomic fingerprinting: Neighbor list

Simple Example: Single component trimer

POSCAR

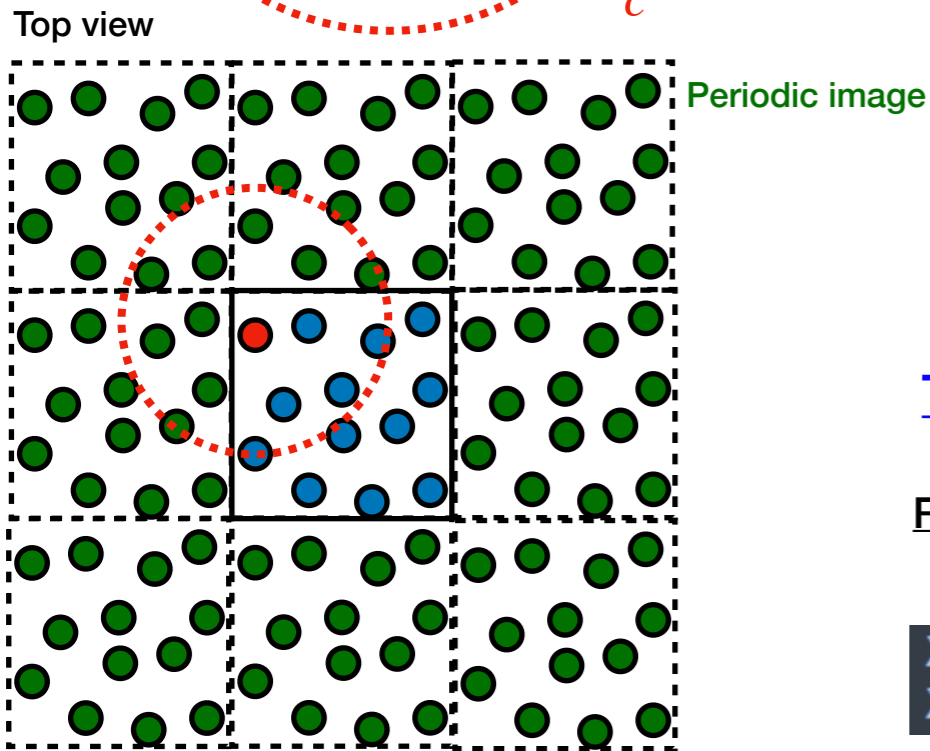


Position vectors
 $\begin{pmatrix} \tilde{x}_0, \tilde{y}_0, \tilde{z}_0 \\ \tilde{x}_1, \tilde{y}_1, \tilde{z}_1 \\ \tilde{x}_2, \tilde{y}_2, \tilde{z}_2 \end{pmatrix}$



Relative to central atom
 $\begin{pmatrix} \tilde{x}_1 - \tilde{x}_0, \tilde{y}_1 - \tilde{x}_0, \tilde{z}_1 - \tilde{x}_0 \\ \tilde{x}_2 - \tilde{x}_0, \tilde{y}_2 - \tilde{x}_0, \tilde{z}_2 - \tilde{x}_0 \end{pmatrix}$

\downarrow
 $X = \begin{pmatrix} x_1, y_1, z_1 \\ x_2, y_2, z_2 \end{pmatrix}$ Neighbor list



Pair terms: $r_{ij} = \left(\sum_{rows} X^2 \right)^{\frac{1}{2}} = \begin{pmatrix} r_{01} \\ r_{02} \end{pmatrix}$

Three body terms: $X_A = \begin{pmatrix} x_1, y_1, z_1 \\ x_1, y_1, z_1 \\ x_2, y_2, z_2 \\ x_2, y_2, z_2 \end{pmatrix}$ $X_B = \begin{pmatrix} x_1, y_1, z_1 \\ x_2, y_2, z_2 \\ x_1, y_1, z_1 \\ x_2, y_2, z_2 \end{pmatrix}$

Replicate and tile the neighbor list

```
Xij=np.tile(nbl,n).reshape(n*n,3)
Xik=np.tile(nbl,(n,1)).reshape(n*n,3)
```

```
rij=((Xij**2.0).sum(axis=1)**0.5).reshape(1,n*n); #sum accros row
rik=((Xik**2.0).sum(axis=1)**0.5).reshape(1,n*n);
cos_ijk1=((Xij*Xik).sum(axis=1).reshape(1,n*n))/rij/rik;
```

supercell

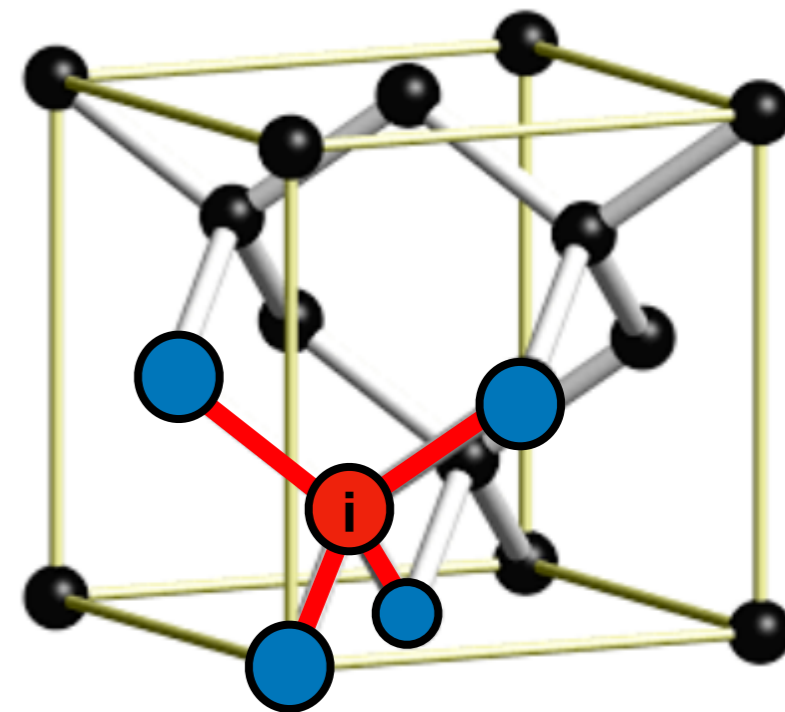
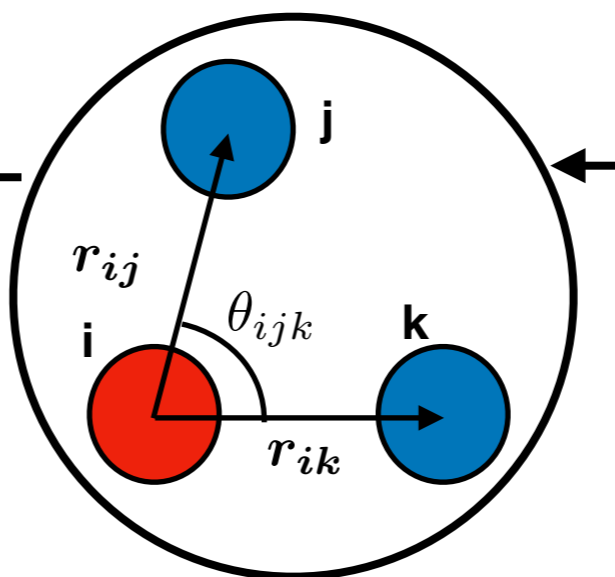
Neighbor list for atom-i

Atomic fingerprinting: LSP Calc

Physically informed artificial neural networks for atomistic modeling of materials GPP Pun, R Batra, R Ramprasad, Y Mishin - Nature communications, 2019

Structure parameters:

$$G_i^{m,n} = \sum_{j,k} P_m(\cos(\theta_{ijk})) f(r_{ij}) f(r_{ik})$$



Angular term:

$$P_m(\cos(\theta)) \quad m = 0, 1, 2, 4, 6$$

(Legendre polynomials)

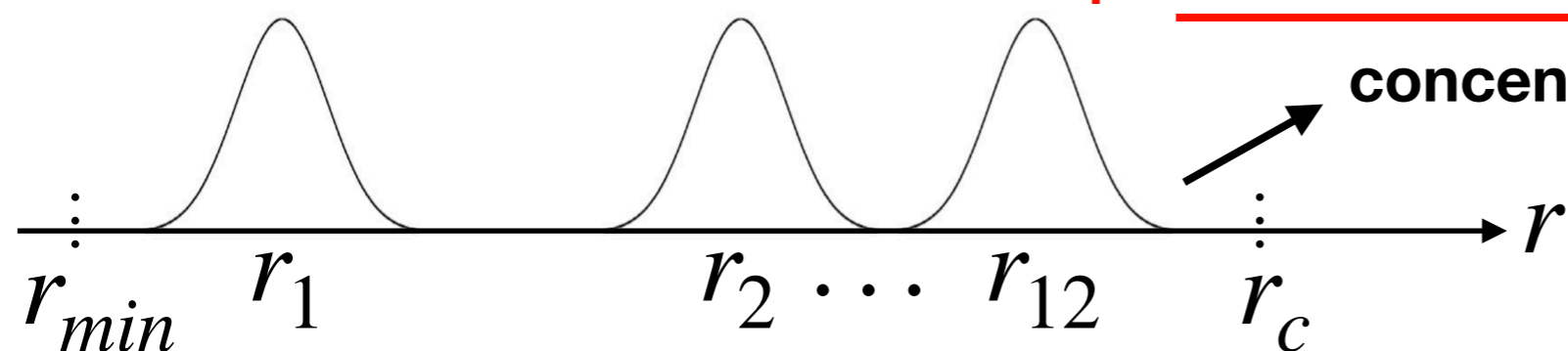
Radial term:

$$f(r) = \frac{1}{r_n} e^{-\frac{(r-r_n)^2}{\sigma^2}} f_c(r)$$

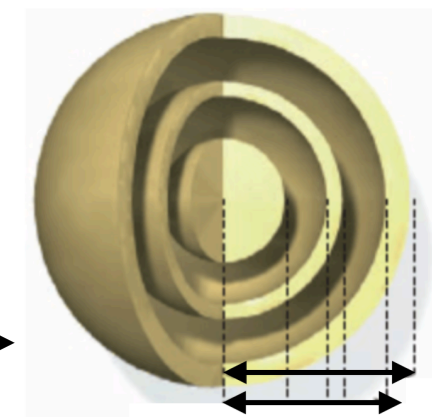
choose 12 values for r_n

$f_c(r)$ = Cutoff function

G_i 's act as "fingerprints" of the local atomic environment



concentric shells



$$f_c(r) = \begin{cases} \frac{(r-r_c)^4}{d^4 + (r-r_c)^4} & r \leq r_c \\ 0, & r \geq r_c \end{cases}$$

PyFit Functionality

★ Current functionality

- Single component mathematical ANN
 - local atomic environment descriptors developed by [Purja-Pun and Mishin](#)

• Beta version

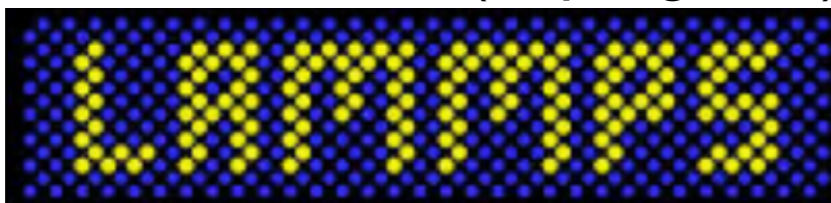
- Single component PINN training
 - local atomic environment descriptors developed by [Purja-Pun and Mishin](#)

• Future plans

- Add Behler-Parrinello LSP for the case of single component ANN
- Multi-component ANN training
- Multi-component PINN training

• Implementation

↓ (in progress)



G. Purja Pun, J. Chapman

ParaGrandMC: PGMCMC

Parallel Grand Canonical Monte Carlo Simulation Code

<https://software.nasa.gov/software/LAR-18773-1>

V. Yamakov

Workflow

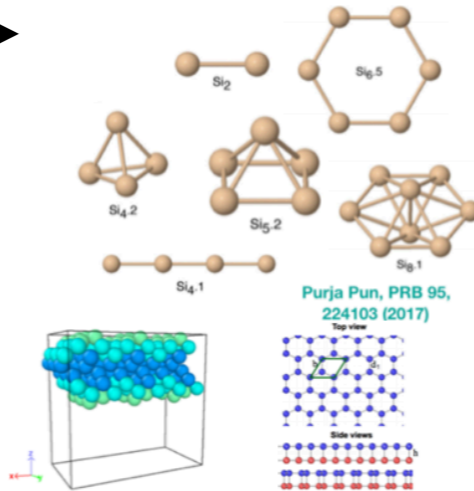
Pre-training

DFT Data Generation

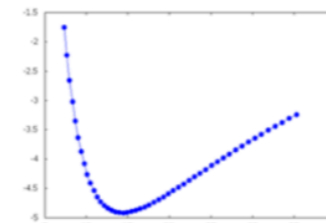
- generated using VASP before training
- K-Point and ENCUT convergence
- Literature comparison
- properties+values

Structural sampling

Large collection of structural prototypes
bulk (FCC, BCC, etc),
defects, 2D, clusters, etc



structural prototype perturbations



- isotropic expansion/compression
- Shearing
- anisotropic expansion/compression
- frozen phonons
- thermal perturbations (AIMD)
- etc

DFT

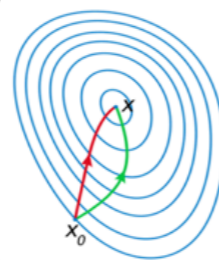
Data set

Structure-1 U_1
Structure-2 U_2
⋮
Structure-M U_M

PyFit

Training loop

L-BFGS (quasi-Newton method)



<u>Training set</u>	<u>DFT energies</u>	<u>Model predictions</u>
Structure-1	U_1	\hat{U}_1
Structure-2	U_2	\hat{U}_2
⋮		
Structure-M	U_M	\hat{U}_M

PyTorch

RMSE error $\epsilon(w) = \sum_j^M \left(\frac{(U_j - \hat{U}_j)^2}{M} \right)^{\frac{1}{2}} \rightarrow \text{Minimize}$

stopping criterion

Pre-processing

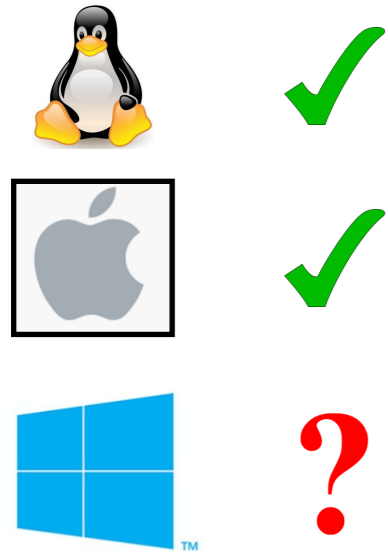
- atomic environment fingerprinting
- error/consistency checks
- matrix construction

Interatomic potential

DEMO

Dependency Installation

Operating systems



Required dependencies



Manual install

```
sudo pip3 install torch torchvision numpy
```



↓
README.md

- 1) **Install conda:** <https://docs.conda.io/projects/conda/en/latest/user-guide/install/>
- 2) **Create conda environment and install dependencies**

```
conda deactivate # exit current conda environment if one is activated
conda create -n TORCH3.7 python=3.7 # create new conda environment named TORCH3.7
conda activate TORCH3.7 # activate the TORCH3.7 environment
conda install -c pytorch pytorch # install the pytorch in the TORCH3.7 environment
conda update --all && conda clean -all # update and clean
```

3) **Clone PyFit demo from GitHub**

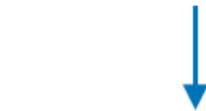
OR <https://github.com/jfh3/PYFIT-FF>

```
git clone https://github.com/jfh3/PYFIT-FF
```

↓ Code ▾

Contents

<https://github.com/jfh3/PYFIT-FF>



PYFIT-FF

NIST license

User manual

PYFIT-Manual.pdf

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examples

src

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ANN

Si ANN potential fitting example

TORCH-EXAMPLES

various instructive PyTorch examples

Source code



data.py

dataset class



defaults.json

Default parameters



neural.py

neural network class



pyfit.py

Main script



reader.py

File reader subroutines



util.py

Miscellaneous subroutines



writer.py

File writer subroutines

Neural network input file

Potential type
flag: ANN=5

optional LSP
shift (default=0)

activation
function
flag

$$0 \rightarrow s(x) = \frac{1}{1 + e^{-x}}$$

$$1 \rightarrow \left(\frac{1}{1 + e^{-x}} \right) - 0.5$$

$$f_c(r) = \begin{cases} \frac{(r - r_c)^4}{d^4 + (r - r_c)^4} & r \leq r_c \\ 0, & r \geq r_c \end{cases}$$

5 0.0 1

1 → Number of elements

Si 28.0855 → Chemical symbol and weight

cut-off parameters

i_{rand} W_{max} r_c d σ ← 0 0.250000 4.500000 1.000000 2.000000

2 0 1 → N_{LG} O_1 $O_2 \dots$

N_{r_o} r_1 $r_2 \dots$ ← 2 2.0 3.0

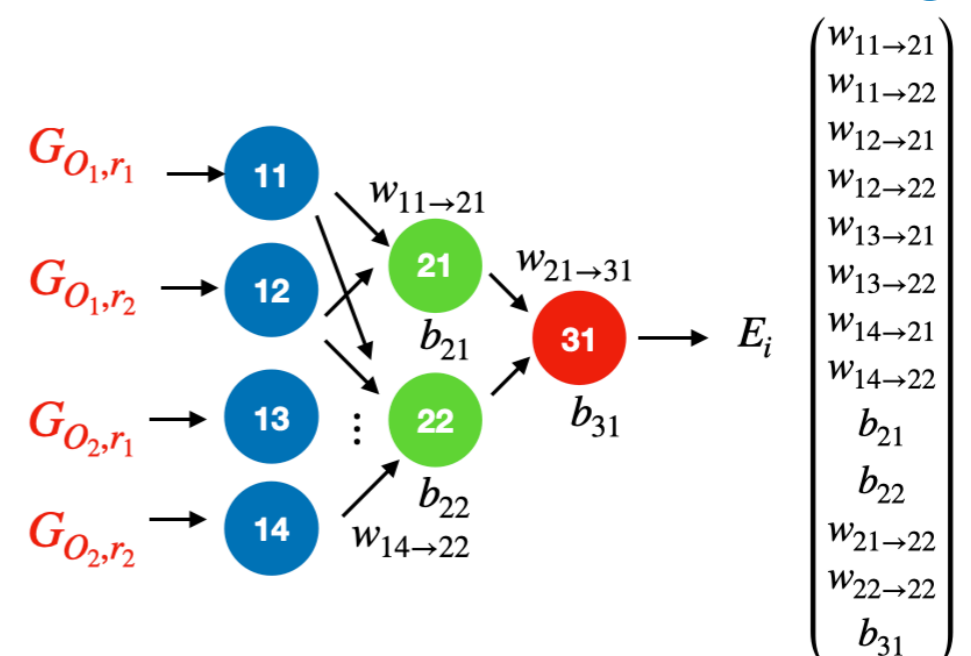
0 0 1 1 1 1 1 1 → Reference parameters

N_{layer} , N_{input} , H_1 H_2 N_{output} ← 3 2 1

w{11} → {21}
w{11} → {22}
w{12} → {21}
⋮

list of NN weights
and bias terms

Neural network ordering



Input file

PYFIT-FF/src/defaults.json

```
{
  "train_RMSE"      : true,
  "rmse_tol"       : 0.00001,
  "dump_poscars"   : false,
  "u_shift"        : 0.795023,
  "ramp_LR"        : true,
  "mid_ramp"       : 10,
  "LR_o"           : 0.01,
  "LR_f"           : 0.10,
  "lambda_Lp"      : 0.00001,
  "LP"             : 2.0,
  "constrain_WB"   : 0.0,
  "test_set_tags"  : ["GRP-BCC-P-UNPERTURBED+ISO"],
  "n_rand_GIDS"    : 0,
  "fix_rand_seed"  : false,
  "exclude_from_test" : ["DC", "ISOLATED", "LIQ"],
  "save_every1"    : 10,
  "save_every2"    : 100,
  "lbfgs_max_iter" : 20,
  "train_edges"    : true,
  "pot_type"       : "NN",
  "pot_file"       : "NN1.dat",
  "dataset_path"   : "train.dat",
  "max_iter"       : 100000,
  "rmse_dU"        : 0.0,
  "rmse_stop"      : 0.002,
  "fraction_train" : 0.8,
  "re_randomize"   : true,
  "weight_selector" : ["DC", "AIMD", "Wurt"],
  "default_weight1" : 1.0,
  "default_weight2" : 0.0,
  "mod_weight1"    : 1.0,
  "mod_weight2"    : 0.0,
  "use_cuda"       : false,
  "dynamic_NN"     : false,
  "start_fresh"    : false,
  "try_n_times"    : 1,
  "lambda_E1"      : 1.0,
  "lambda_dU"      : 1.0,
  "lambda_L1"      : 0.0,
  "cnst_final_bias" : true,
  "final_bias"     : 0.0,
  "write_lsp"      : true,
  "normalize_gi"    : false,
  "normalize_by_ro" : false,
  "normalize_ei"    : false
}
```

PYFIT-FF/examples/MMN/input.json

```
{
  "pot_type"       : "NN",
  "pot_file"       : "NN0.dat",
  "dataset_path"   : "train.dat",
  "u_shift"        : 0.795023,
  "test_set_tags"  : ["GRP-BCC-P-UNPERTURBED+ISO"],
  "fraction_train" : 0.8,
  "dump_poscars"   : false,
  "ramp_LR"        : true,
  "mid_ramp"       : 10,
  "LR_o"           : 0.01,
  "LR_f"           : 0.10,
  "lambda_Lp"      : 0.00001,
  "LP"             : 2.0,
  "train_RMSE"     : true,
  "rmse_tol"       : 0.00001,
  "max_iter"       : 100000,
  "rmse_stop"      : 0.002,
  "save_every1"    : 10,
  "save_every2"    : 100,
  "weight_selector" : ["DC", "AIMD", "Wurt"],
  "default_weight1" : 2.0,
  "train_edges"    : true,
  "use_cuda"       : false,
  "pot_type"       : "NN",
  "pot_file"       : "NN1.dat",
  "dataset_path"   : "train.dat",
  "rmse_dU"        : 0.0,
  "re_randomize"   : true
}
```

Output files

```
(MBP3.7) james@james-VirtualBox:~/HOME/SRC/PY-FIT/PYFIT-FF/examples/MNN$ ls
input.json      PF-e_vs_V-no_dft-0.dat    PF-e_vs_V-test-100.dat    PF-e_vs_V-validate-0.dat    PF-LSP.dat    PF-stats-test.dat    pyfit
NN0.dat        PF-e_vs_V-no_dft-100.dat  PF-e_vs_V-train-0.dat     PF-e_vs_V-validate-100.dat  PF-NN-0.dat   PF-stats-train.dat    RUN.sh
PF-err-log.dat PF-e_vs_V-test-0.dat     PF-e_vs_V-train-100.dat  PF-log.dat                  PF-NN-100.dat PF-stats-validate.dat  train.dat
```

- **e_vs_v files:**

- As the name suggests these files contain volume vs energy data for the various structures. Each dataset, i.e. training, validation, and test, will get its own file. The naming convention is , for example 00-e_vs_v-test-1000.dat. The first column is the volume per atom in the structure (V/N), the second column is the energy per atom DFT energy (E_{DFT}/N).

- **err file:**

- This file is a simple columnar text file which reports various terms of the objective function as function of the iteration step. This file only reports metrics associated with the training set, metrics associated with other data sets are reported in the stat files described below. The frequency at which the values are written is controlled by the `save_every` parameter in the `input.json` file, see sec.3.4.2. If a particular term in the objective function is not being used then it will be reported as a zero in the file.

- **stat files:**

- These files describe the statistical state of the training process and contain various error metrics of the various data sets; training, validation, test.

- **NN files:**

- The code periodically writes the current state of the neural network to a “NN” file using the naming convention “PREFIX-NN-STEP.dat” where STEP refers the training iteration,

Run Example