MODELING DIFFUSION MOBILITIES IN THE L12 AND B2 PHASES

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May 14, 2007

Microstructure Evolution



Kim and Walter, Mater. Sci. Eng. A360 (2003) 7.

Need to calculate multicomponent diffusion simulations: $\gamma/B2 \longrightarrow \gamma/\gamma /B2$

γ+γ / B2+γ γ+γ /γ /B2+γ

Ni-Al System

➢ Ni-Al Assessment from Ansara et al. (1997).



 γ' (Ni₃Al): L1₂ base structure; metal sublattice contains a connected network for nearest neighbor jumps for vacancies

B2 (NiAl) CsCl structure: metal sublattice requires jumps between different sublattices.

Effect of chemical ordering on diffusion

$$M_{i} = \frac{M_{i}^{\circ}}{RT} \exp\left(\frac{-\Delta Q_{i}}{RT}\right) \text{ where } \Delta Q_{i} = f(c_{i},T) \text{ and } M_{i}^{\circ} = f(c_{i},T)$$

• Based on Bragg-Williams approach by Girifalco for a binary system (*J. Phys. Chem. Solids*, 1964, **24**, 323.)

 $\Delta Q_k = \Delta Q_k^{dis} \left[1 + \alpha_k \left(S^{ord} \right)^2 \right] \qquad S^{ord} = p_A^{\alpha} - p_A^{\beta} = \text{long-range order parameter}$

 p_A^{α} is the probability of finding A atom on an α site

• Expansion to Multicomponent systems Helander and Ågren, (Acta Mater., 1999, 47, 1141.)

$$\Delta Q = \Delta Q^{\text{dis}} + \Delta Q^{\text{ord}}$$
$$\Delta Q_{l}^{ord} = \sum_{i} \sum_{j} \Delta Q_{i:j}^{ord} \left[y_{i}^{\alpha} y_{j}^{\beta} - x_{i} x_{j} \right]$$
$$+ \sum_{i} \sum_{j} \sum_{k} \Delta Q_{ij:k}^{ord} \left[y_{i}^{\alpha} y_{j}^{\alpha} y_{k}^{\beta} - x_{i} x_{j} x_{k} \right]$$
$$+ \sum_{i} \sum_{j} \sum_{k} \Delta Q_{k:ij}^{ord} \left[y_{i}^{\beta} y_{j}^{\beta} y_{k}^{\alpha} - x_{i} x_{j} x_{k} \right]$$

 ΔQ_{ij}^{ord} = contribution to activation energy for component *k* as a result of the ordering of *i*-*j* atoms

$$y_i^{\alpha} = \frac{N_i^{\alpha}}{N_{tot}^{\alpha}} = p_i^{\alpha}$$

Before assessing the diffusion mobilities need consider thermodynamics

DICTRA



- If one uses Ni-Data (Thermotech) Convert γ and B2
- If one uses a database based Ni-AI by Dupin et. al. Convert B2
- ✓ Can convert phase descriptions to a MSL description (Dupin et al.)
 - only works if element does not have a stable BCC phase

Phase Field

 Thermodynamics do not necessarily need to match diffusion description, depends on model used

Assessment of diffusion in NiAl

- B2 (Ni,Cr)AI (Ni,AI,Cr,Va:AI,Ni,Cr,Va)
- Thermodynamics from N. Dupin, I. Ansara, B. Sundman, CALPHAD, 25, (2001) 279-298

Disorder description fixed Engstrom and Ågren assessment 1996

$$M_{i} = \frac{M_{i}^{\circ}}{RT} \exp\left(\frac{-\Delta Q_{i}^{*}}{RT}\right) \text{ where } \Delta Q_{i}^{*} = f(c_{i}, T)$$

Disorder Description

$$\Delta Q_{Ni}^{*} = x_{Ni}Q_{Ni}^{Ni} + x_{Al}Q_{Al}^{Ni} + x_{Cr}Q_{Cr}^{Ni} + x_{Al}x_{Ni}Q_{Al,Ni}^{Ni} + x_{Cr}x_{Ni}Q_{Cr,Ni}^{Ni}$$

$$\Delta Q_{Al}^{*} = x_{Ni}Q_{Ni}^{Al} + x_{Al}Q_{Al}^{Al} + x_{Cr}Q_{Cr}^{Al} + x_{Al}x_{Ni}Q_{Al,Ni}^{Al}$$

$$\Delta Q_{Cr}^{*} = x_{Ni}Q_{Ni}^{Cr} + x_{Al}Q_{Al}^{Cr} + x_{Cr}Q_{Cr}^{Cr} + x_{Cr}x_{Ni}Q_{Cr,Ni}^{Cr}$$

Assessment of diffusion in NiAl

- B2 (Ni,Cr)Al (Ni,Al,Cr,Va:Al,Ni,Cr,Va)
- Thermodynamics from N. Dupin, I. Ansara, B. Sundman, CALPHAD, 25, (2001) 279-298

Disorder description fixed Engstrom and Ågren assessment 1996

$$M_{i} = \frac{M_{i}^{\circ}}{RT} \exp\left(\frac{-\Delta Q_{i}^{*}}{RT}\right) \text{ where } \Delta Q_{i}^{*} = f(c_{i}, T)$$

Order Description

$$\Delta Q_{Ni}^{ord} = \Delta Q_{Al:Ni}^{ord} \left[y_{Al}^{Ni} y_{Ni}^{Al} - x_{Al} x_{Ni} \right] + \Delta Q_{Ni:Al}^{ord} \left[y_{Ni}^{Ni} y_{Al}^{Al} - x_{Al} x_{Ni} \right] + \Delta Q_{Al:Va}^{ord} \left[y_{Al}^{Ni} y_{Va}^{Al} - x_{Al} x_{Va} \right] + \Delta Q_{Va:Al}^{ord} \left[y_{Va}^{Ni} y_{Al}^{Al} - x_{Va} x_{Al} \right] + \Delta Q_{Ni:Va}^{ord} \left[y_{Ni}^{Ni} y_{Va}^{Al} - x_{Ni} x_{Va} \right] + \Delta Q_{Va:Ni}^{ord} \left[y_{Ni}^{Ni} y_{Va}^{Al} - x_{Va} x_{Ni} \right] + \Delta Q_{Al:Cr}^{ord} \left[y_{Ni}^{Ni} y_{Va}^{Al} - x_{Ni} x_{Cr} \right] + \Delta Q_{Va:Ni}^{ord} \left[y_{Ni}^{Ni} y_{Va}^{Al} - x_{Al} x_{Cr} \right] + \Delta Q_{Cr:Va}^{ord} \left[y_{Cr}^{Ni} y_{Va}^{Al} - x_{Cr} x_{Va} \right] + \Delta Q_{Va:Cr}^{ord} \left[y_{Va}^{Ni} y_{Cr}^{Al} - x_{Va} x_{Cr} \right] + \Delta Q_{Cr:Ni}^{ord} \left[y_{Cr}^{Ni} y_{Ni}^{Al} - x_{Cr} x_{Ni} \right] + \Delta Q_{Ni:Cr}^{ord} \left[y_{Ni}^{Ni} y_{Cr}^{Al} - x_{Cr} x_{Ni} \right]$$

Assessed Mobility Parameters for B2 - NiAlCr

Mobility Parameters	Value
Ni	
$\Delta Q_{Ni:Al} = \Delta Q_{Ni:Al} = \Delta Q_{Cr:Al} = \Delta Q_{Cr:Al}$	-336810
$\Delta Q_{Al:Va} = \Delta Q_{Va:Al}$	-115600
$\Delta Q_{Ni:Cr} = \Delta Q_{Ni:Cr}$	-255690
Al	
$\Delta Q_{Ni:Al} = \Delta Q_{Ni:Al} = \Delta Q_{Cr:Al} = \Delta Q_{Cr:Al}$	-360140
$\Delta Q_{Al:Va} = \Delta Q_{Va:Al}$	+305900
$\Delta Q_{Ni:Cr} = \Delta Q_{Ni:Cr}$	-6220700
Cr	
$\Delta Q_{Ni:Al} = \Delta Q_{Ni:Al} = \Delta Q_{Cr:Al} = \Delta Q_{Cr:Al}$	-336810
$\Delta Q_{Al:Va} = \Delta Q_{Va:Al}$	-115600
$\Delta Q_{Ni:Cr} = \Delta Q_{Ni:Cr}$	1148100

Composition and Temperature Dependence of B2 Interdiffusion Coefficient







Composition Dependence of B2 Interdiffusion Activation Energy



Self Diffusion of Ni in NiAl



Assessment of diffusion mobilities in Ni₃Al

L1₂ (Ni₃Al) (Ni,Al:Ni,Al)

Disorder description fixed Engstrom and Ågren assessment 1996

$$M_{i} = \frac{M_{i}^{\circ}}{RT} \exp\left(\frac{-\Delta Q_{i}^{*}}{RT}\right) \text{ where } \Delta Q_{i}^{*} = f(c_{i}, T)$$

$$\Delta Q_{Ni}^{*} = x_{Ni}Q_{Ni}^{Ni} + x_{Al}Q_{Al}^{Ni} + x_{Cr}Q_{Cr}^{Ni} + x_{Al}x_{Cr}Q_{Al,Cr}^{Ni} + x_{Cr}x_{Ni}Q_{Cr,Ni}^{Ni}$$

$$\Delta Q_{Al}^{*} = x_{Ni}Q_{Ni}^{Al} + x_{Al}Q_{Al}^{Al} + x_{Cr}Q_{Cr}^{Al} + x_{Al}x_{Ni}Q_{Al,Ni}^{Ni} + x_{Cr}x_{Ni}Q_{Cr,Ni}^{Al}$$

$$\Delta Q_{Cr}^{*} = x_{Ni}Q_{Ni}^{Cr} + x_{Al}Q_{Al}^{Cr} + x_{Cr}Q_{Cr}^{Cr} + x_{Al}x_{Ni}Q_{Al,Ni}^{Cr} + x_{Al}x_{Cr}Q_{Al,Cr}^{Cr} + x_{Cr}x_{Ni}Q_{Cr,Ni}^{Cr}$$

 $\begin{aligned} & \Delta Q_{Ni}^{ord} = \Delta Q_{Al:Ni}^{ord} \left[y_{Al}^{Ni} y_{Ni}^{Al} - x_{Al} x_{Ni} \right] + \Delta Q_{Ni:Al}^{ord} \left[y_{Ni}^{Ni} y_{Al}^{Al} - x_{Al} x_{Ni} \right] \\ & + \overline{\Delta Q_{Al:Cr}^{ord}} \left[y_{Al}^{Ni} y_{Cr}^{Al} - x_{Al} x_{Cr} \right] + \overline{\Delta Q_{Cr:Al}^{ord}} \left[y_{Cr}^{Ni} y_{Al}^{Al} - x_{Al} x_{Cr} \right] \\ & \Delta Q_{Cr:Ni}^{ord} \left[y_{Cr}^{Ni} y_{Ni}^{Al} - x_{Cr} x_{Ni} \right] + \Delta Q_{Ni:Cr}^{ord} \left[y_{Ni}^{Ni} y_{Cr}^{Al} - x_{Ni} x_{Cr} \right] \\ & + \overline{\Delta Q_{Al,Ni:Al}^{ord}} \left[y_{Al}^{Ni} y_{Ni}^{Ni} y_{Al}^{Al} - x_{Al} x_{Ni} x_{Al} \right] + \Delta Q_{Al:Al,Ni}^{ord} \left[y_{Al}^{Ni} y_{Ni}^{Al} y_{Al}^{Al} - x_{Al} x_{Al} x_{Ni} \right] \\ & + \Delta Q_{Al,Ni:Ni}^{ord} \left[y_{Al}^{Ni} y_{Ni}^{Ni} y_{Al}^{Al} - x_{Al} x_{Ni} x_{Ni} \right] + \Delta Q_{Ni:Al,Ni}^{ord} \left[y_{Ni}^{Ni} y_{Ni}^{Al} - x_{Ni} x_{Al} x_{Ni} \right] \end{aligned}$

Assessed Mobility Parameters of Ni₃Al

Mobility Parameters	Value
Ni	
$\Delta Q_{Ni:Al} = \Delta Q_{Ni:Al} = \Delta Q_{Cr:Al} = \Delta Q_{Cr:Al} = \Delta Q_{Cr:Ni} = \Delta Q_{Cr:Ni}$	-101530-23.6*T
$\Delta Q_{Al,Ni:Al}^{ord} = \Delta Q_{Al:Al,Ni}^{ord}$	-311700
$\Delta Q_{Al,Ni:Al}^{ord} = \Delta Q_{Al:Al,Ni}^{ord}$	-24870
Al	
$\Delta Q_{Ni:Al} = \Delta Q_{Ni:Al} = \Delta Q_{Cr:Al} = \Delta Q_{Cr:Al} = \Delta Q_{Cr:Ni} = \Delta Q_{Cr:Ni}$	78533-59.1*T
$\Delta Q_{Al,Ni:Al}^{ord} = \Delta Q_{Al:Al,Ni}^{ord}$	869000
$\Delta Q_{Al,Ni:Al}^{ord} = \Delta Q_{Al:Al,Ni}^{ord}$	-127130
Cr	
$\Delta Q_{Ni:Al} = \Delta Q_{Ni:Al}$	-36844
$\Delta Q_{Cr:Al} = \Delta Q_{Cr:Al} = \Delta Q_{Cr:Ni} = \Delta Q_{Cr:Ni}$	-101530-23.6*T

Temperature and Composition Dependence of Ni Tracer Diffusivity in γ $\hat{\gamma}$



B2 Diffusion Couple at 1200 °C for 40 h Ni-35.5Al-3.7Cr at. % / Ni-33.5Al-5.7 Cr at. %



Hopfe, Son, Morral, Romig, Diffusion in Ordered Alloys, TMS (1993) 69.

Diffusion Coefficient Composition Dependence in the Ni-Al system at 1200 °C



Effect of Cr addition Ni-48Al (at.%) at 1200 °C on Diffusivities in the B2 phase



γ/B2 Diffusion Couple Ni-40Al-5Cr/Ni-15Al-20Cr at. %





Test: B2/Ni Simulation



Experimental data from J-C Zhao, GE-CRD

Does the Thermodynamic Database Make a Difference?



Ultimate Goal



E. Perez, T. Patterson, Y. Sohn, J. Phase Equil. Diff., 27 (2006) 659.