

# Square-Root Diffusivity Method

## RPI MatLab<sup>©</sup> Code

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# Outline

- Introduction
- Background & Needs
  - *Profiler*, a DOS code (M.K. Stalker, J.E. Morral)
  - *Acta Materialia*, **51**, 1181-1193, 2003 (MEG & AL)
- RPI's MatLab<sup>©</sup> Multicomponent Diffusion Code
- Testing the code:
  - » 10% Cr –10 %Al –80 %Ni
  - » 43.5% Ni –25 %Zn –31.5 %Cu
  - » 42% Ni –39 %Al – 19% Fe
  - » 32.39% Fe–49.41% Mg–18.20% Ca
- Results



# RPI Matlab<sup>©</sup> Code: GUI

ZFP\_Fn\_GUI\_2

D-Matrix

Values

D 11: 7.8      D 12: 2.5  
D 21: 2.5      D 22: 11

Power

$10^{\text{-}10}$

$\frac{\text{cm}^2}{\text{s}}$

Diffusion-Time

Hours  
(Default time is 1000 hrs)

Temperature

Kelvin  
(Default time is 1000 K)

Chemical Elements

Element 1: Symbol: Cr      At.% of left member alloy: 10 %  
Element 2: Symbol: Al      At.% of left member alloy: 10 %  
Element 3: Symbol: Ni

Angle

ZFP Angle  
 Select

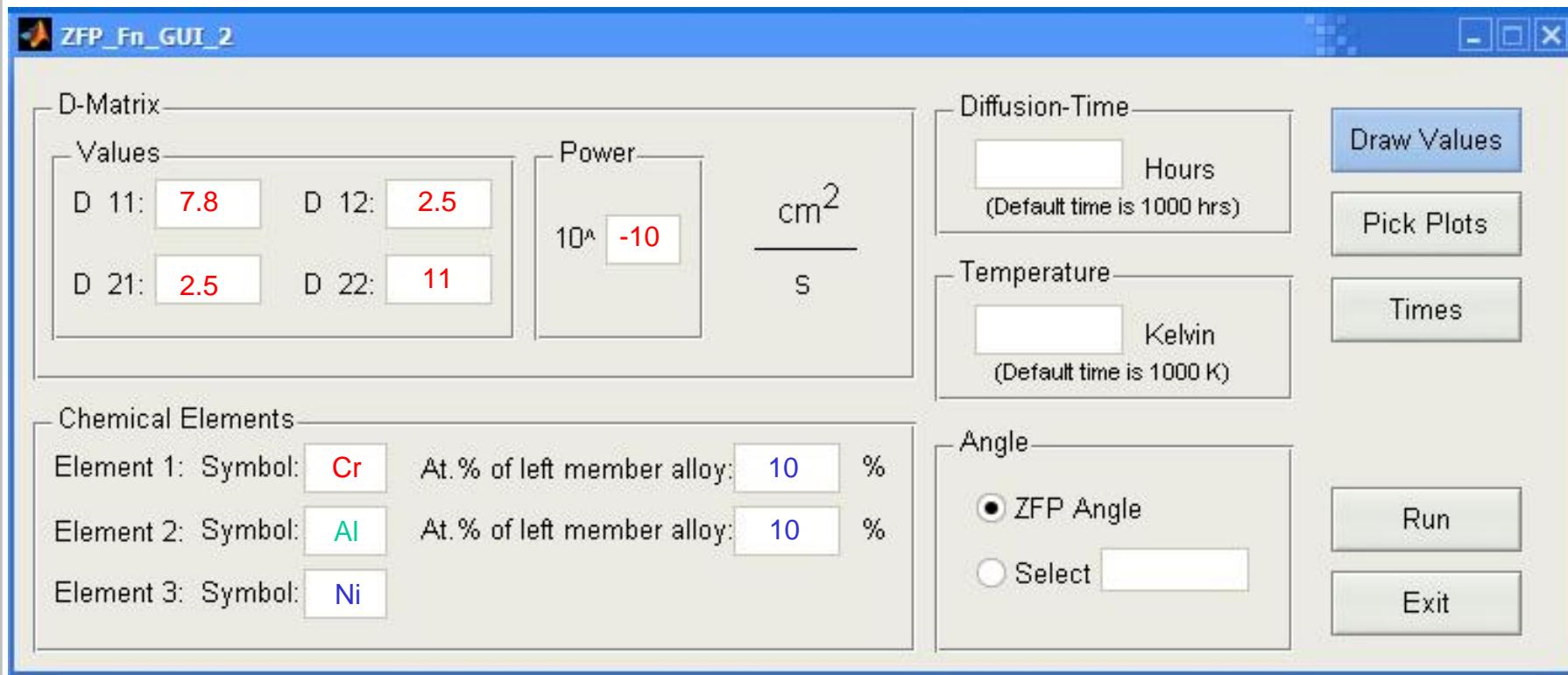
Draw Values

Pick Plots

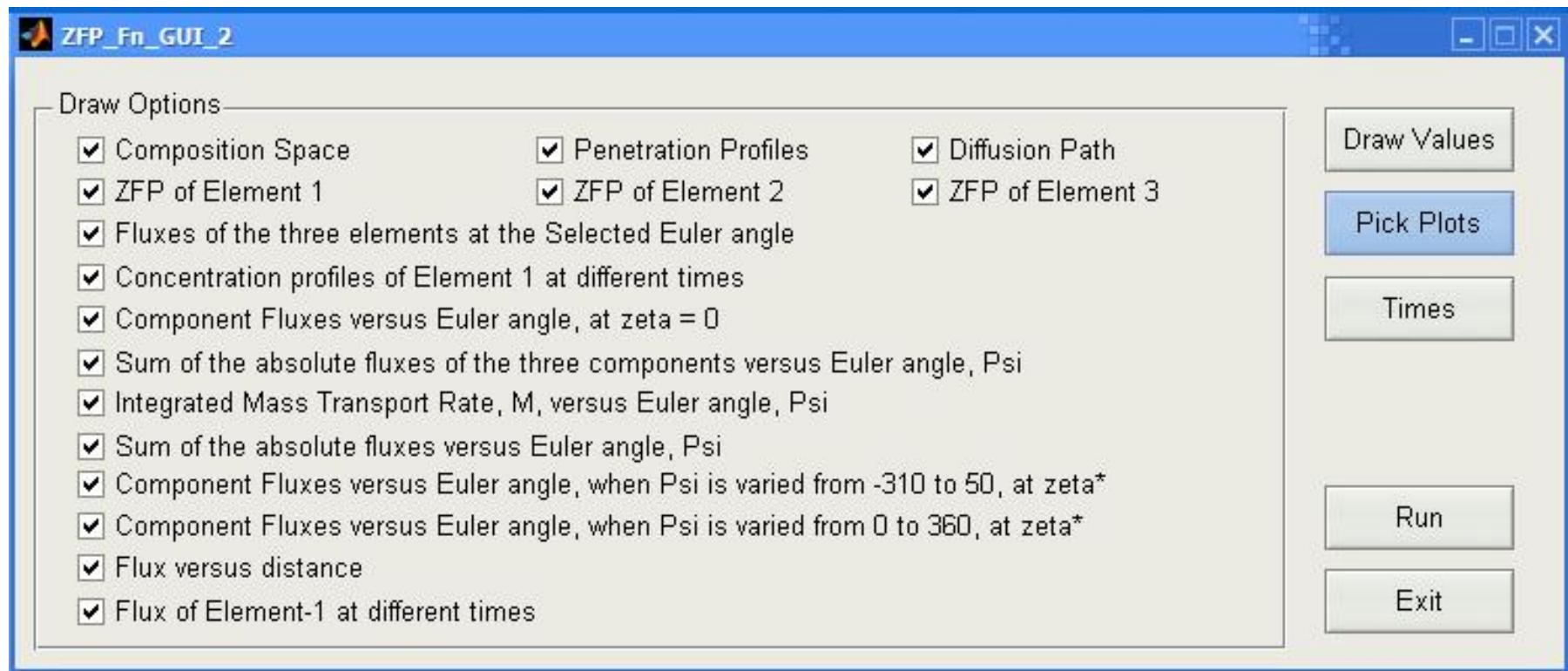
Times

Run

Exit



# RPI Matlab<sup>©</sup> Code: GUI



# RPI Matlab<sup>©</sup> Code: GUI

ZFP\_Fn\_GUI\_2

Times

Times to plot the Concentration Profile of Component 1

Enter the time t1:  Hours (Default time is 20 hrs)

Enter the time t2:  Hours (Default time is 200 hrs)

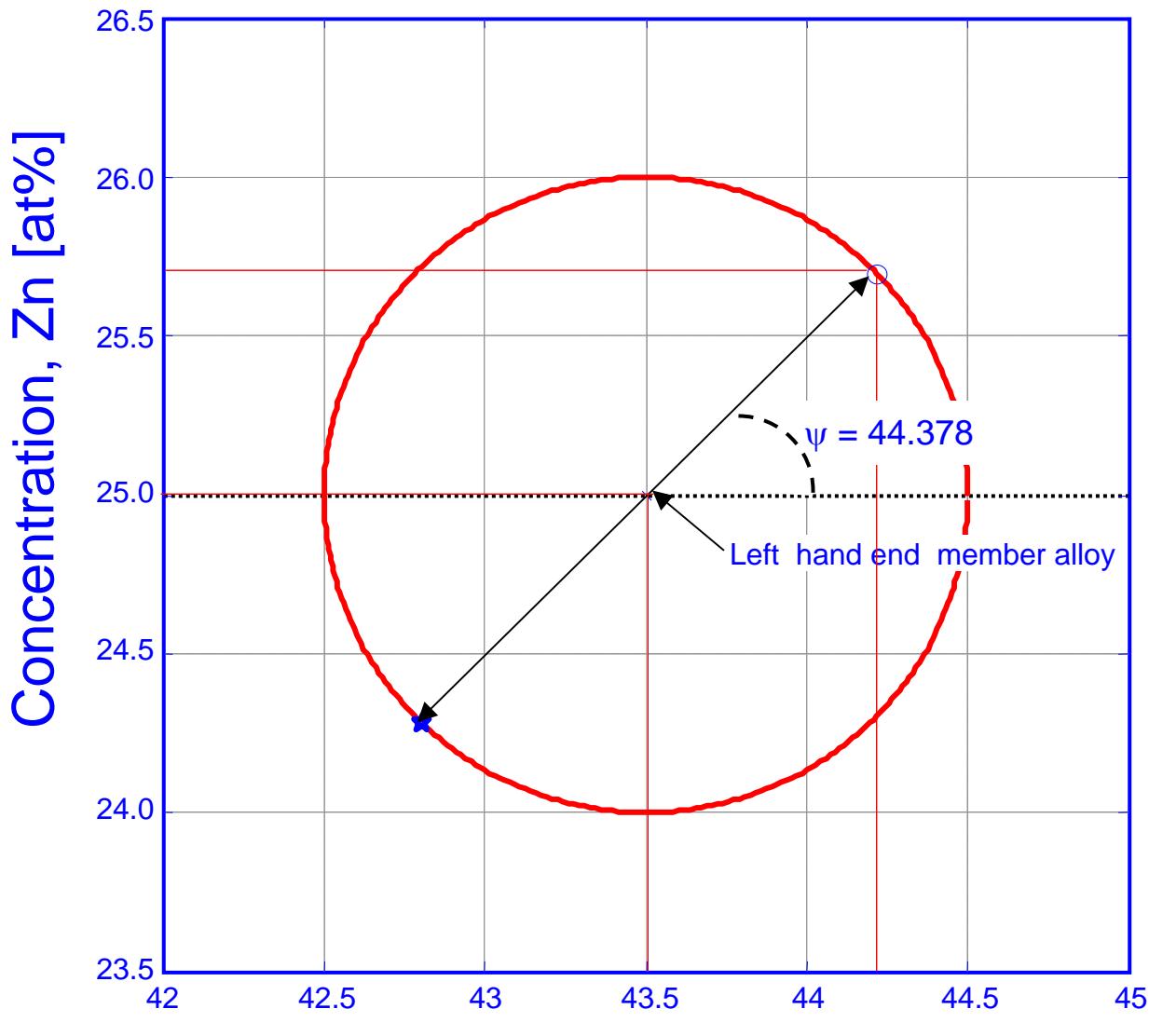
Enter the time t3:  Hours (Default time is 2000 hrs)

Enter the time t4:  Hours (Default time is 5000 hrs)

Enter the time t5:  Hours (Default time is 20000 hrs)

Enter the time t6:  Hours (Default time is 200000 hrs)





## Composition Space

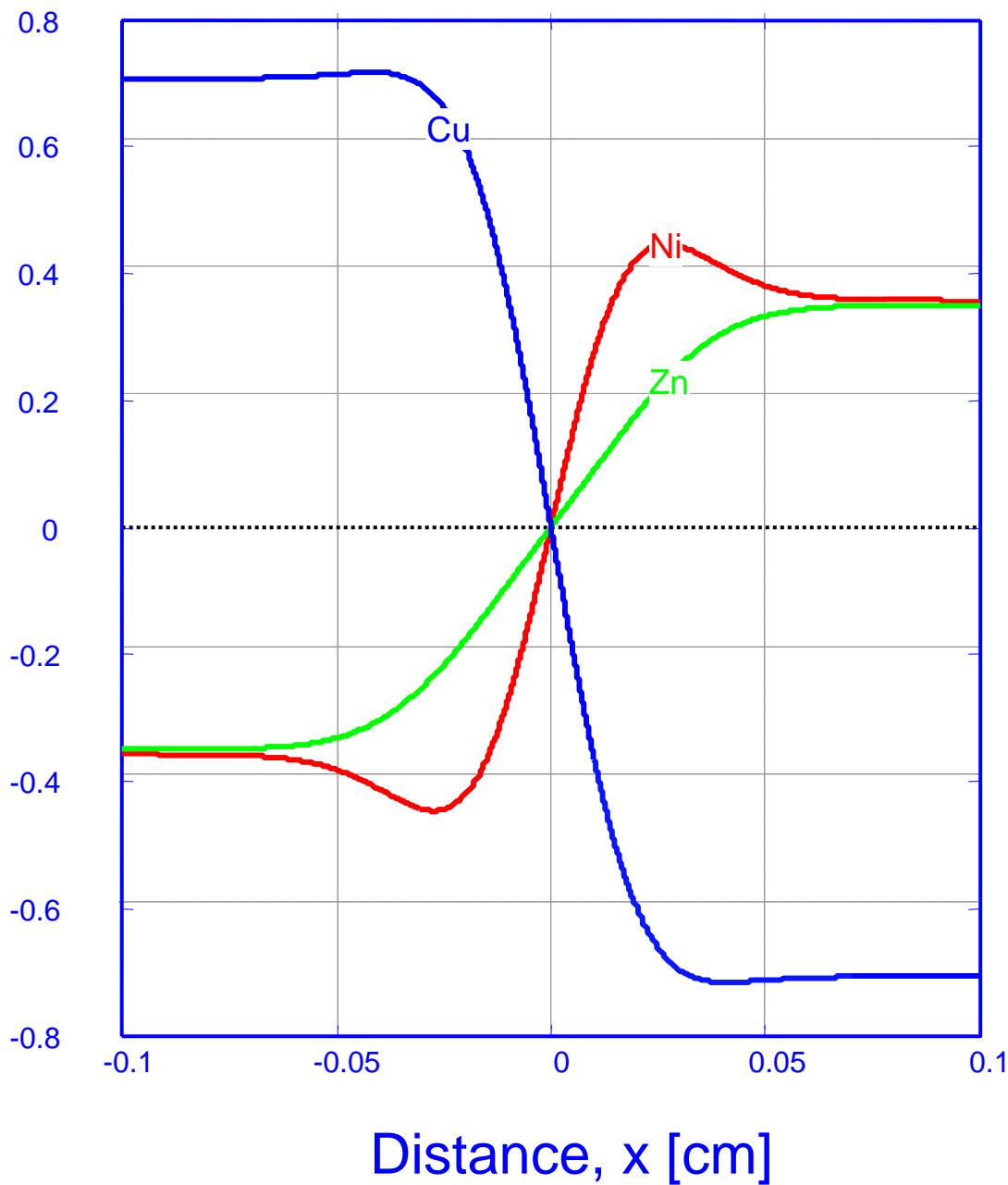
Ni=43.5, Zn=25,  
Cu=31.5 [at%]

T=1048 K

t= 48 h

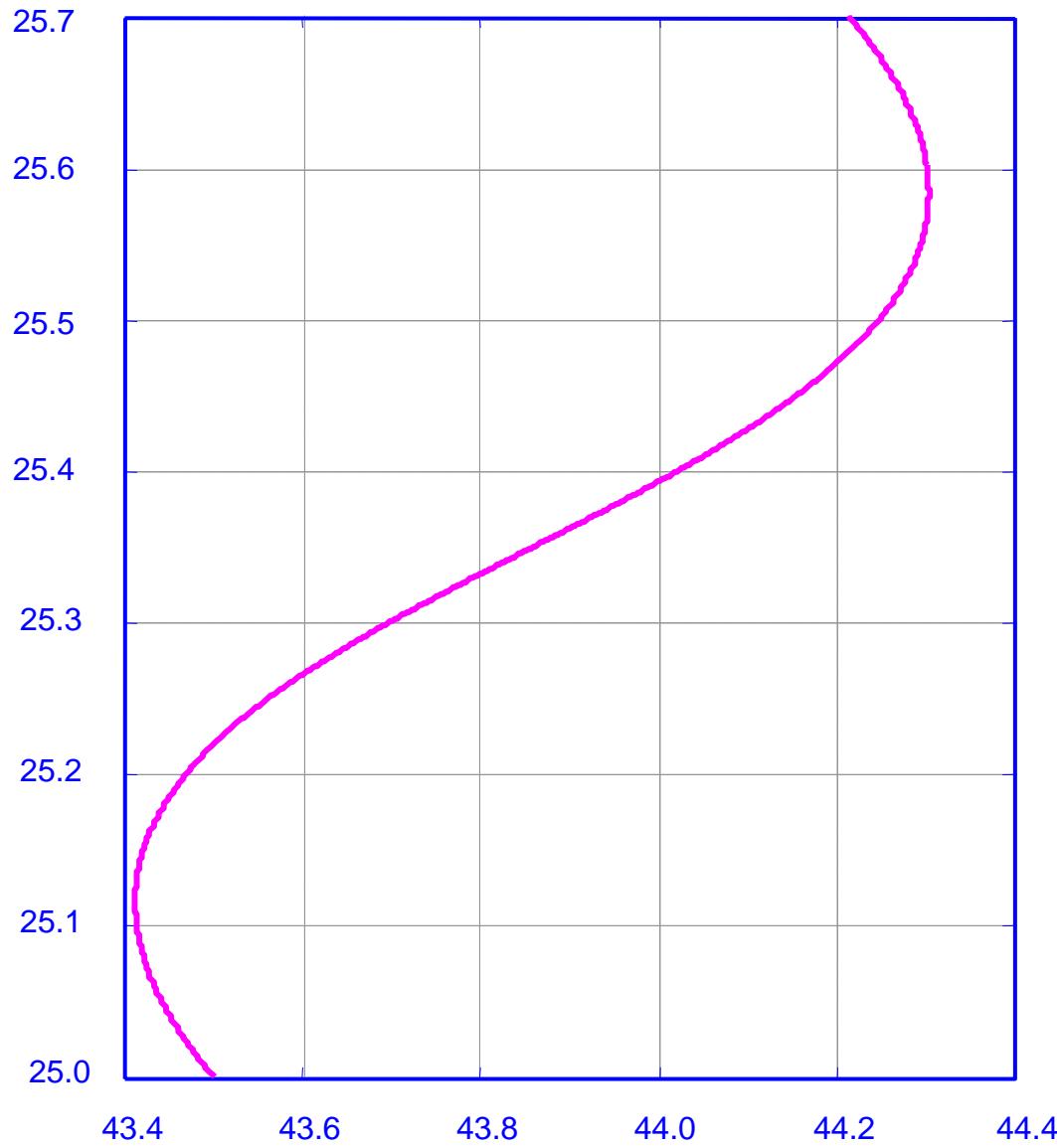


Concentration Difference, [at%]



## Penetration Profiles

Concentration, Zn, [at%]



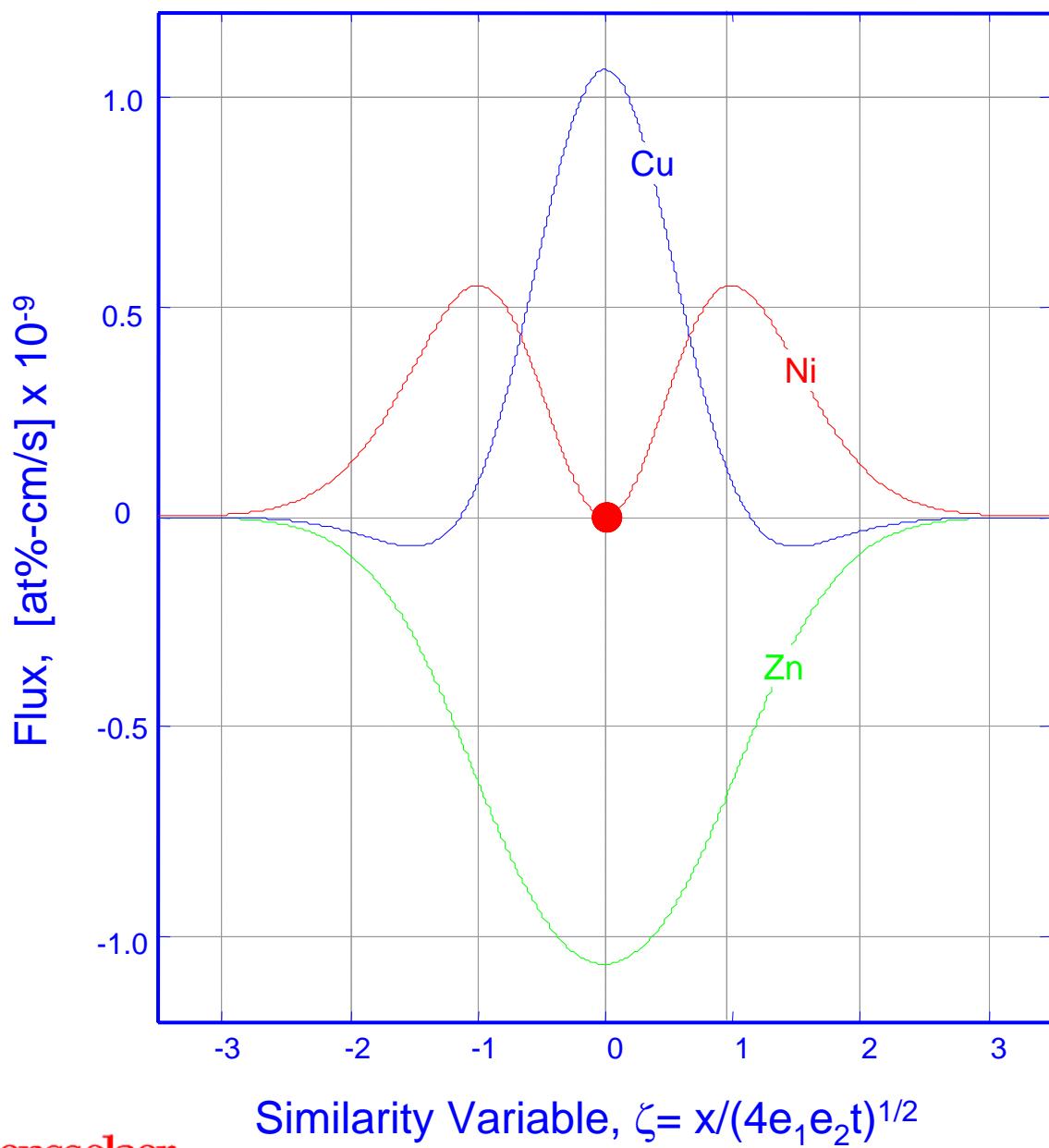
Diffusion  
Path

Concentration, Ni, [at%]



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Stationary  
ZFP for Ni

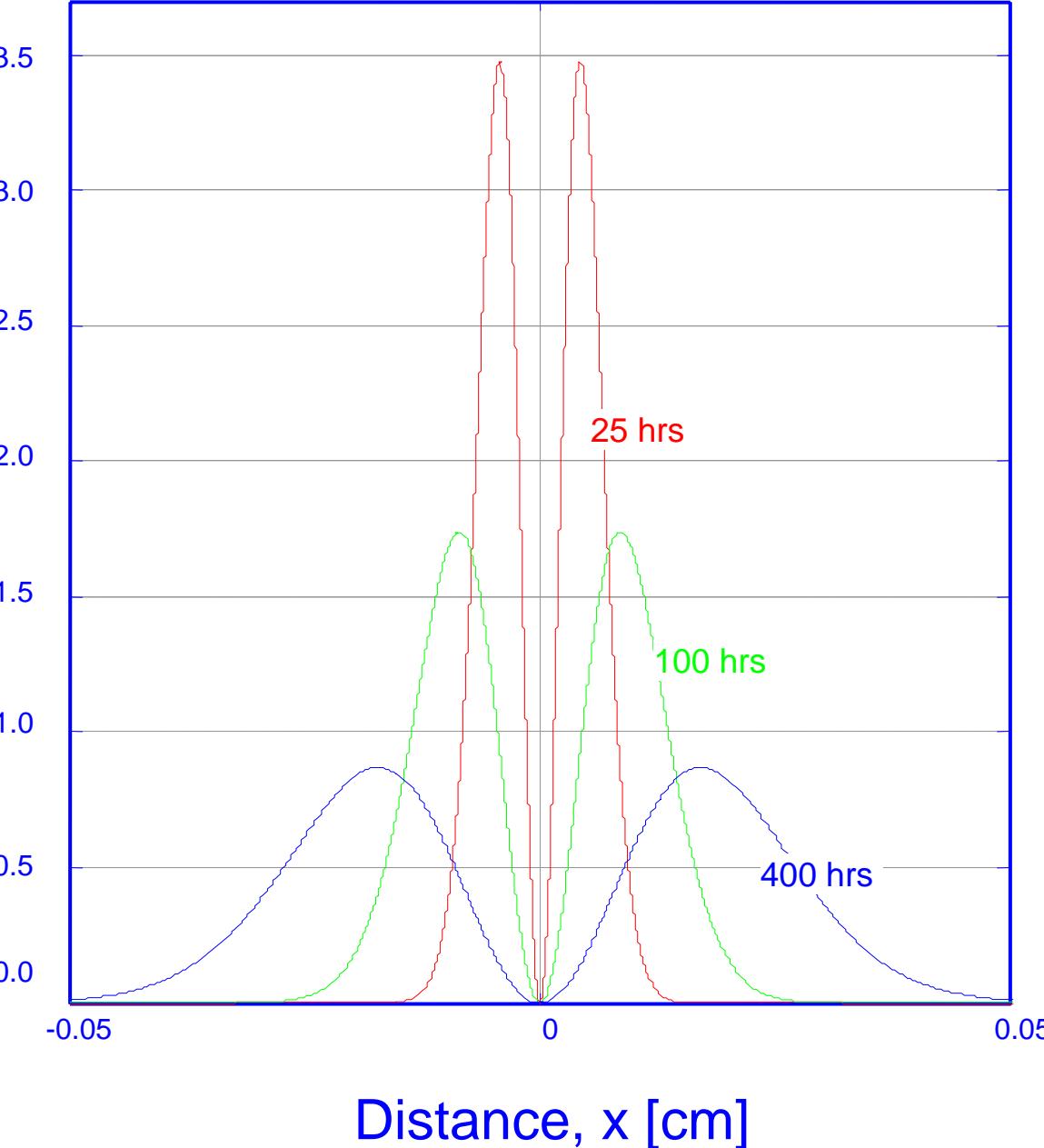
$$\psi = 44.378^\circ$$

## Ni Flux at Different Times

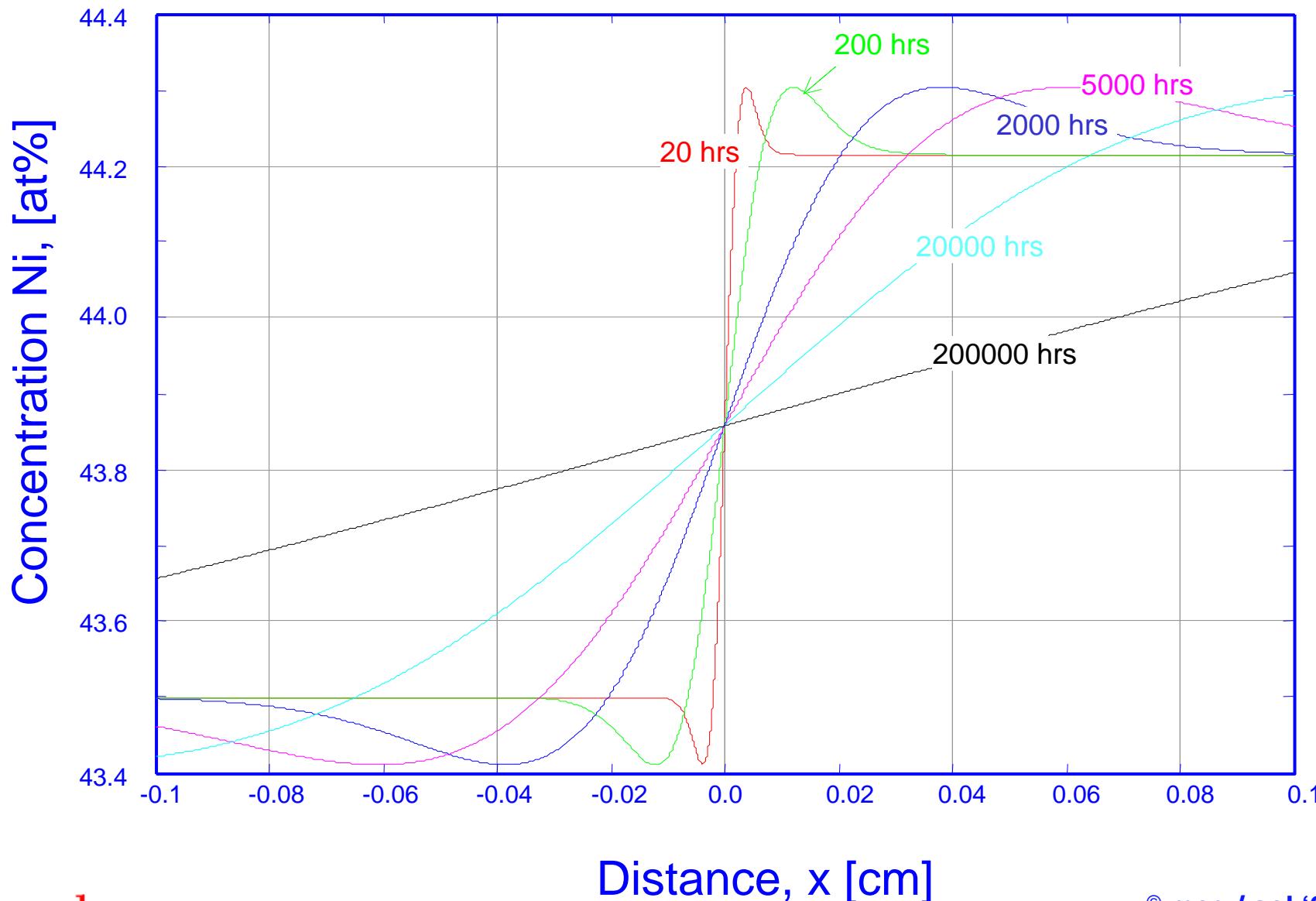
$$\psi = 44.378^\circ$$

$$\zeta = 0$$

Flux of Ni, [at%·cm/s] × 10<sup>-9</sup>

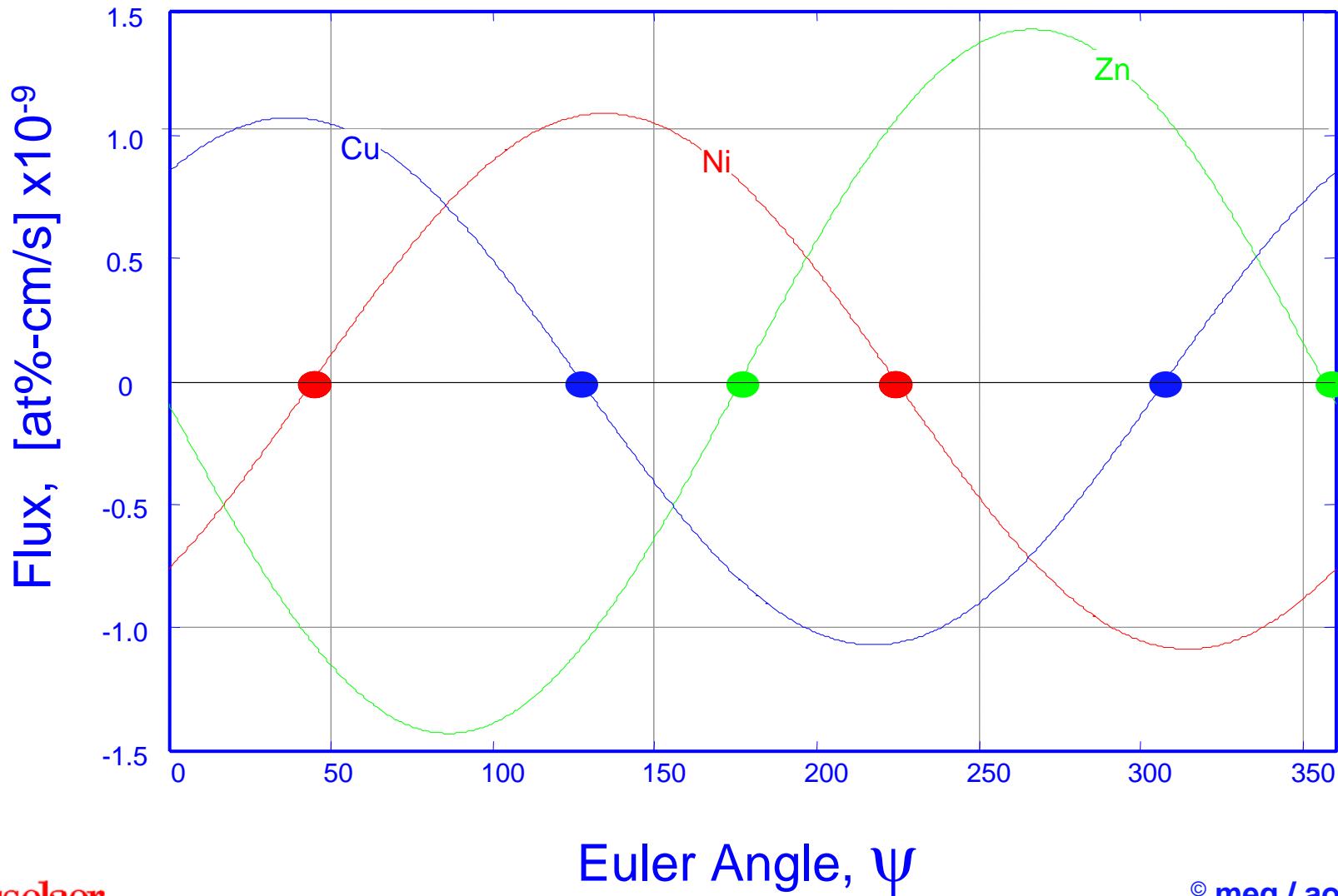


# Concentration Profiles for Ni at Different Times



# Component Fluxes vs. $\psi$

$\zeta = 0$



# Integrated Mass Concept

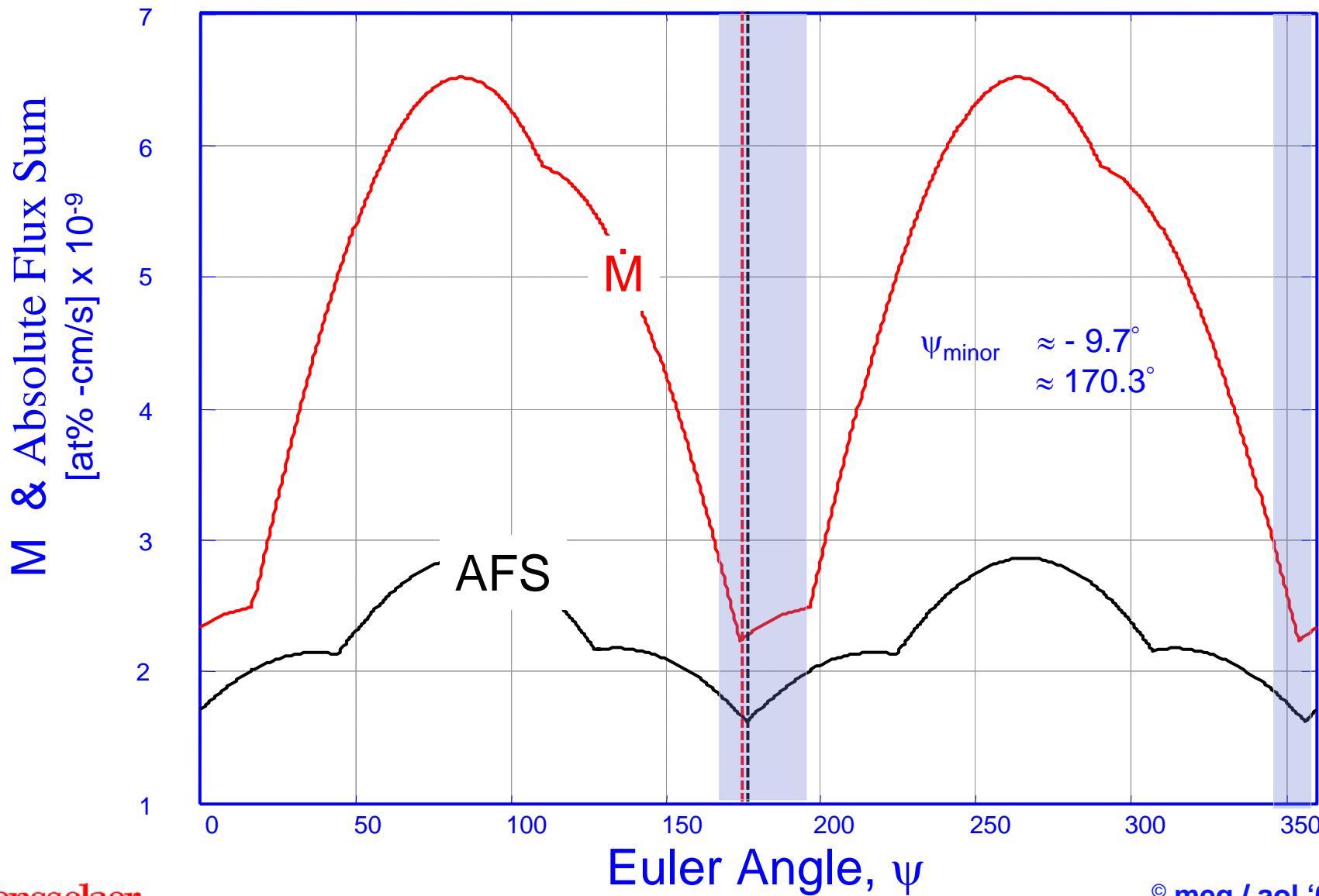
- The absolute transport rate for a ternary diffusion zone

$$M \left| \begin{matrix} & & 3 \\ & J_i & | \\ i & 1 & d \end{matrix} \right.$$

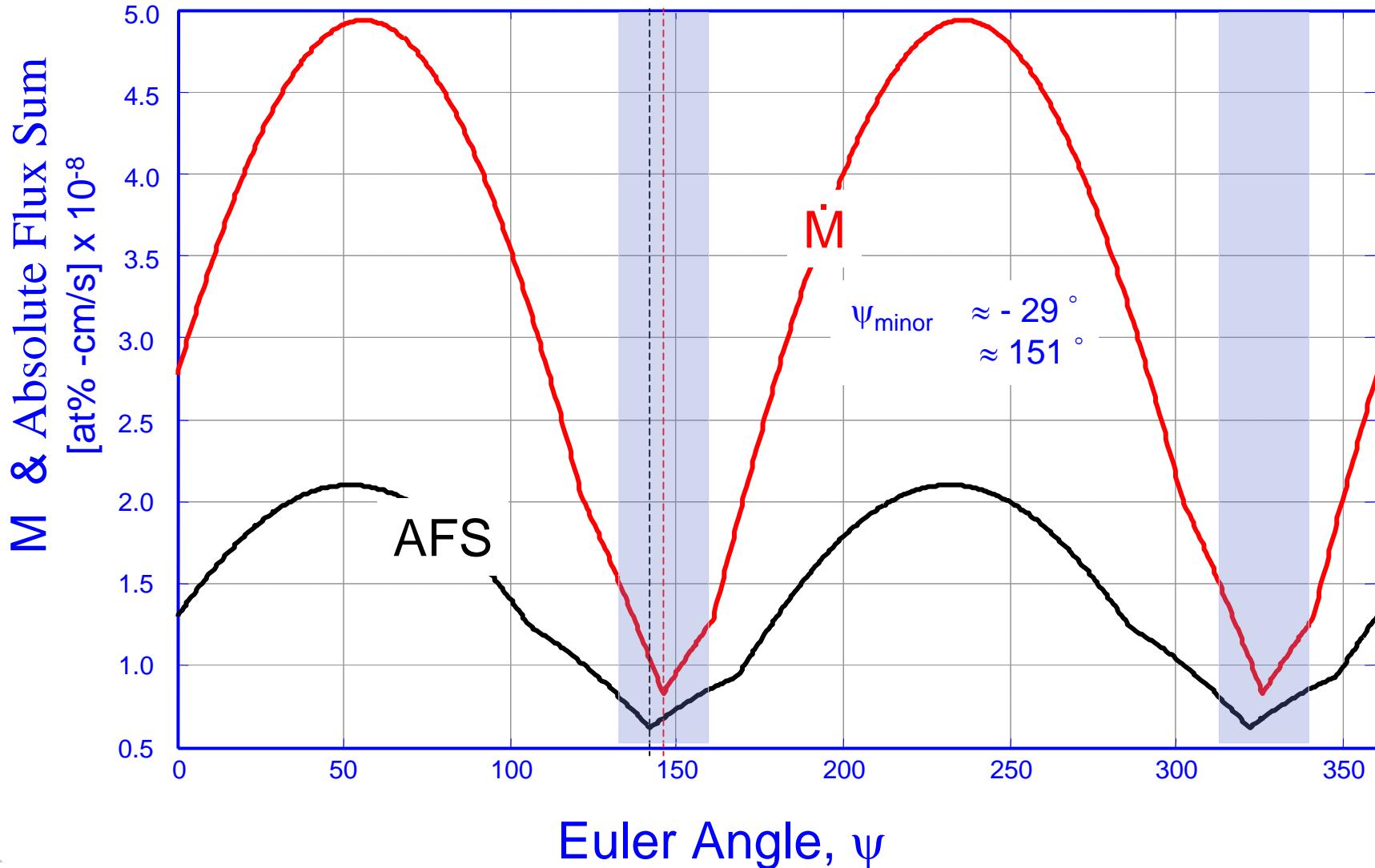
- Carrying out the integration

$$M \frac{1}{\sqrt{e_1 e_2 t}} \left| \begin{matrix} D_{11} & A_{11} & A_{12} & D_{12} & A_{21} & A_{22} \\ D_{11} & D_{21} & A_{11} & A_{12} & D_{12} & D_{22} \end{matrix} \right| \left| \begin{matrix} D_{21} & A_{11} & A_{12} & D_{22} & A_{21} & A_{22} \\ A_{21} & A_{22} \end{matrix} \right|$$

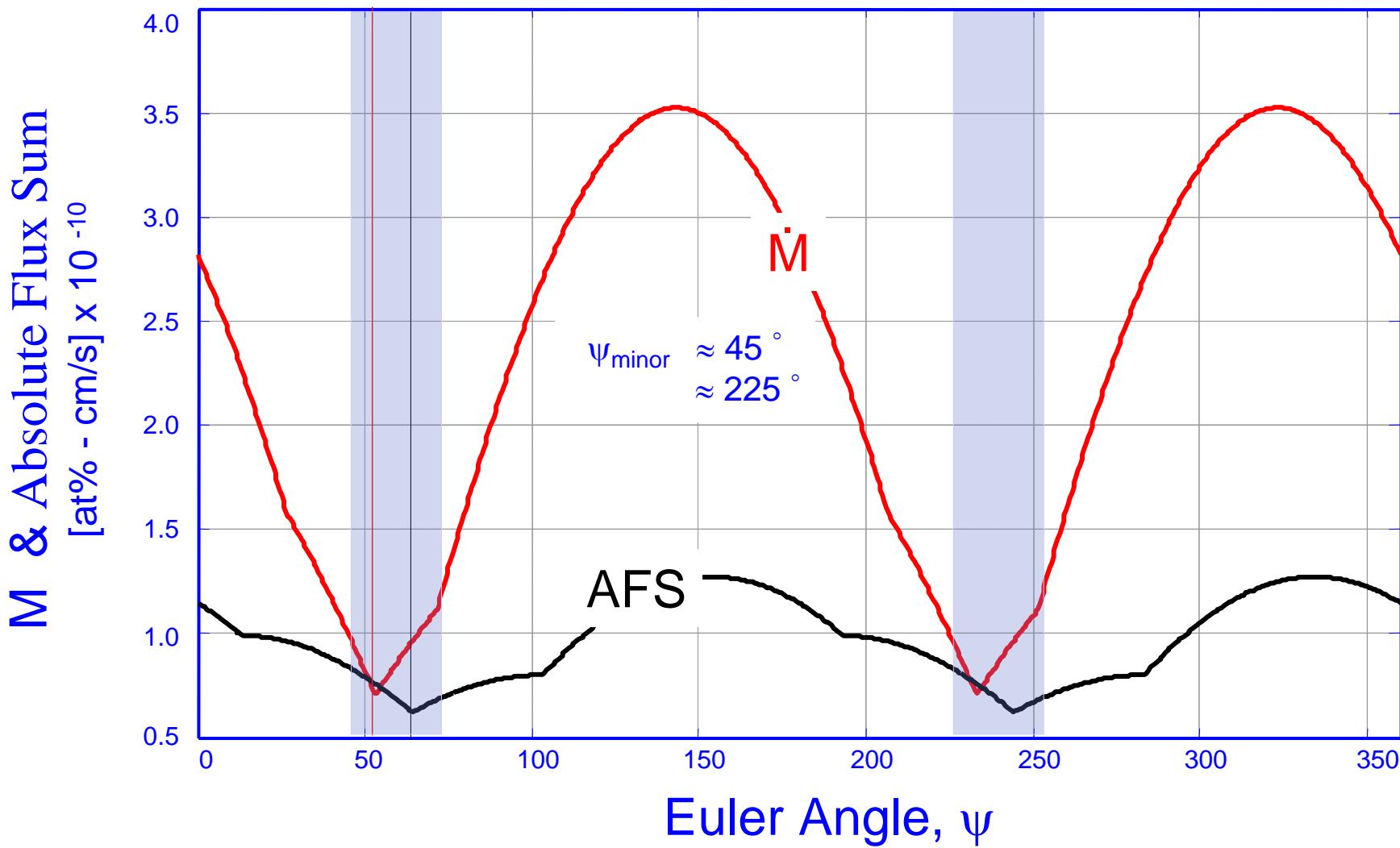
# Ni–43.5, Zn–25, Cu–31.5 [at%]



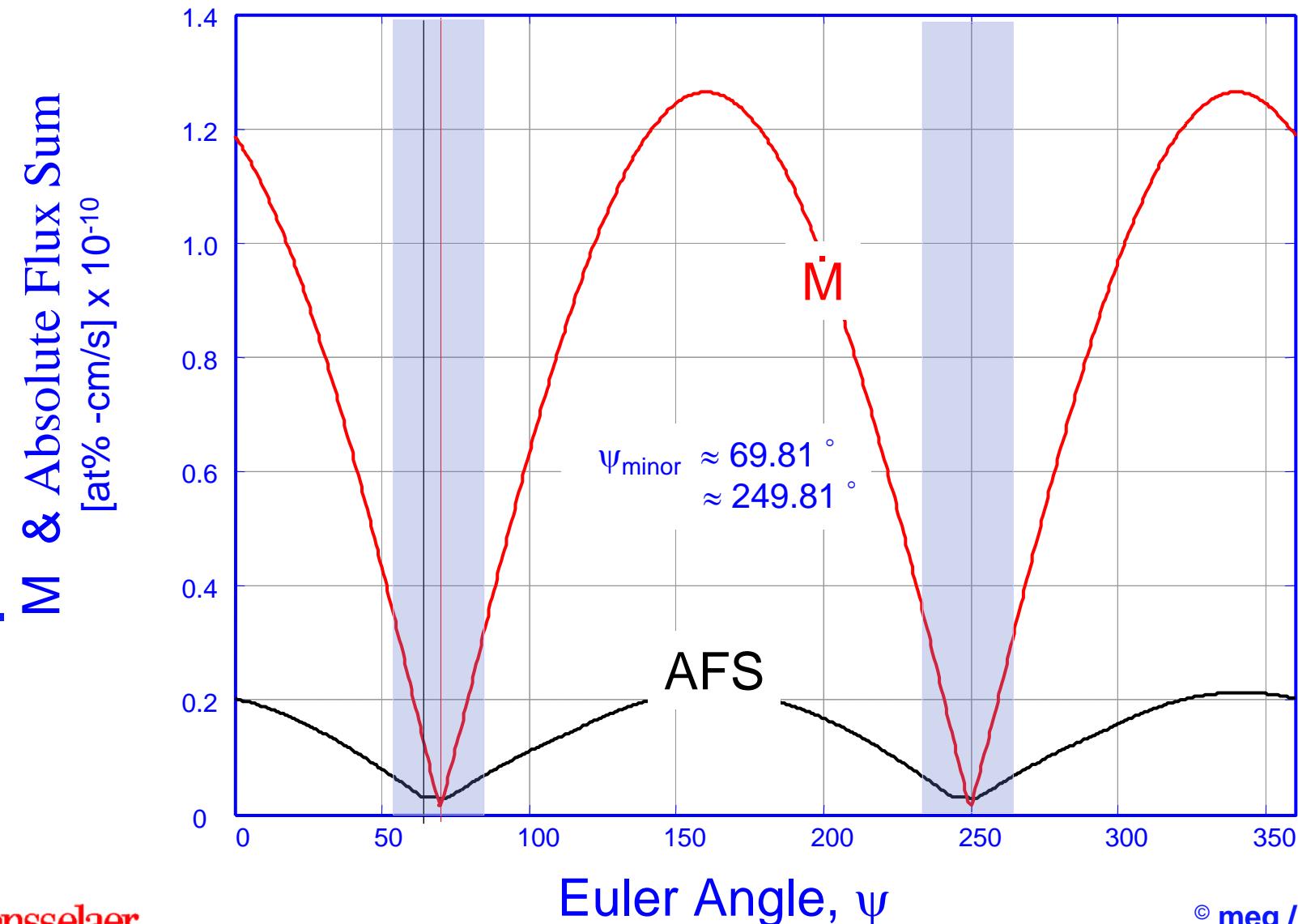
# Cr-10, Al-10, Ni-80 [at%]



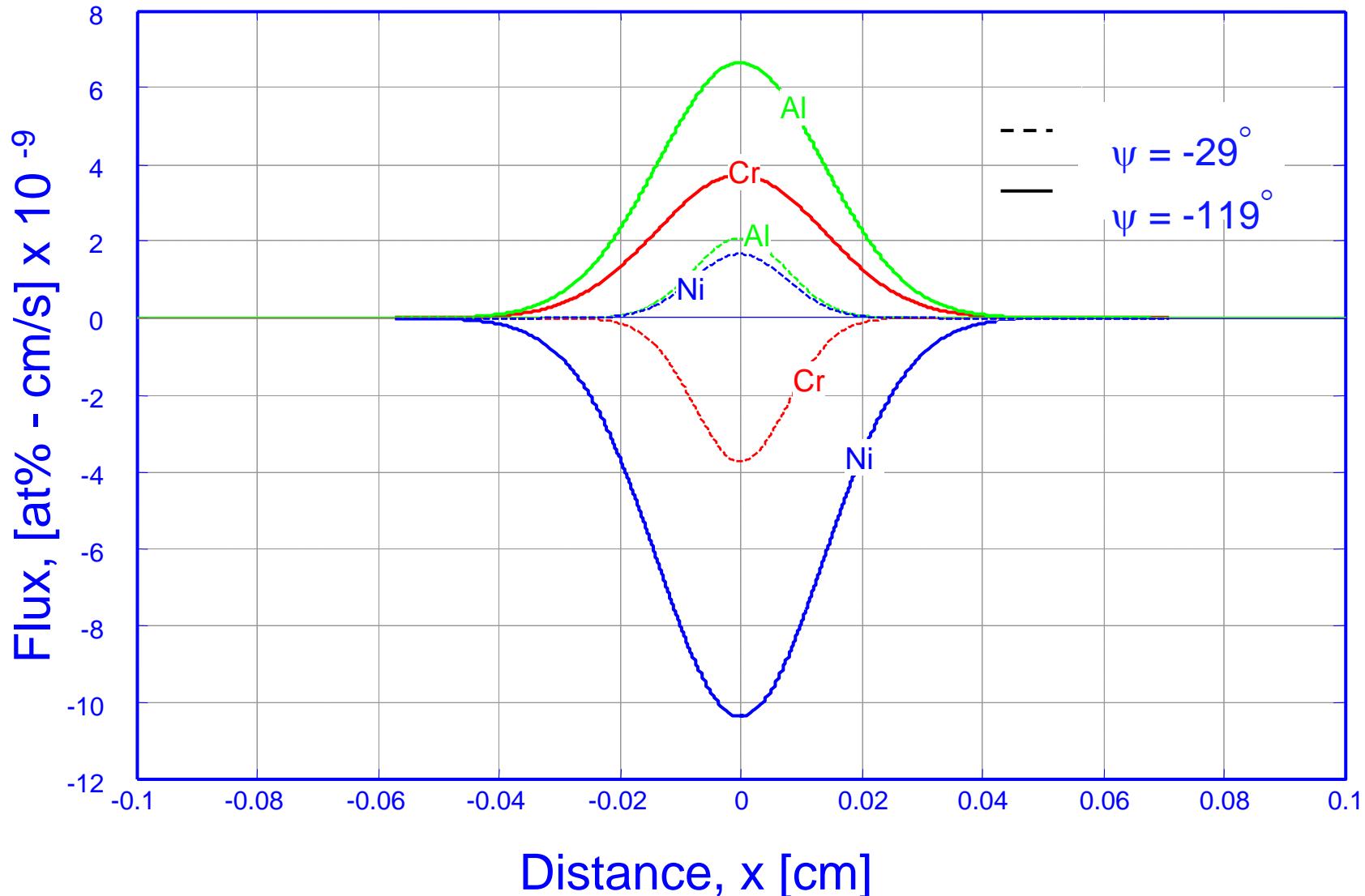
# Ni-42, Al-39, Fe-19 [at%]



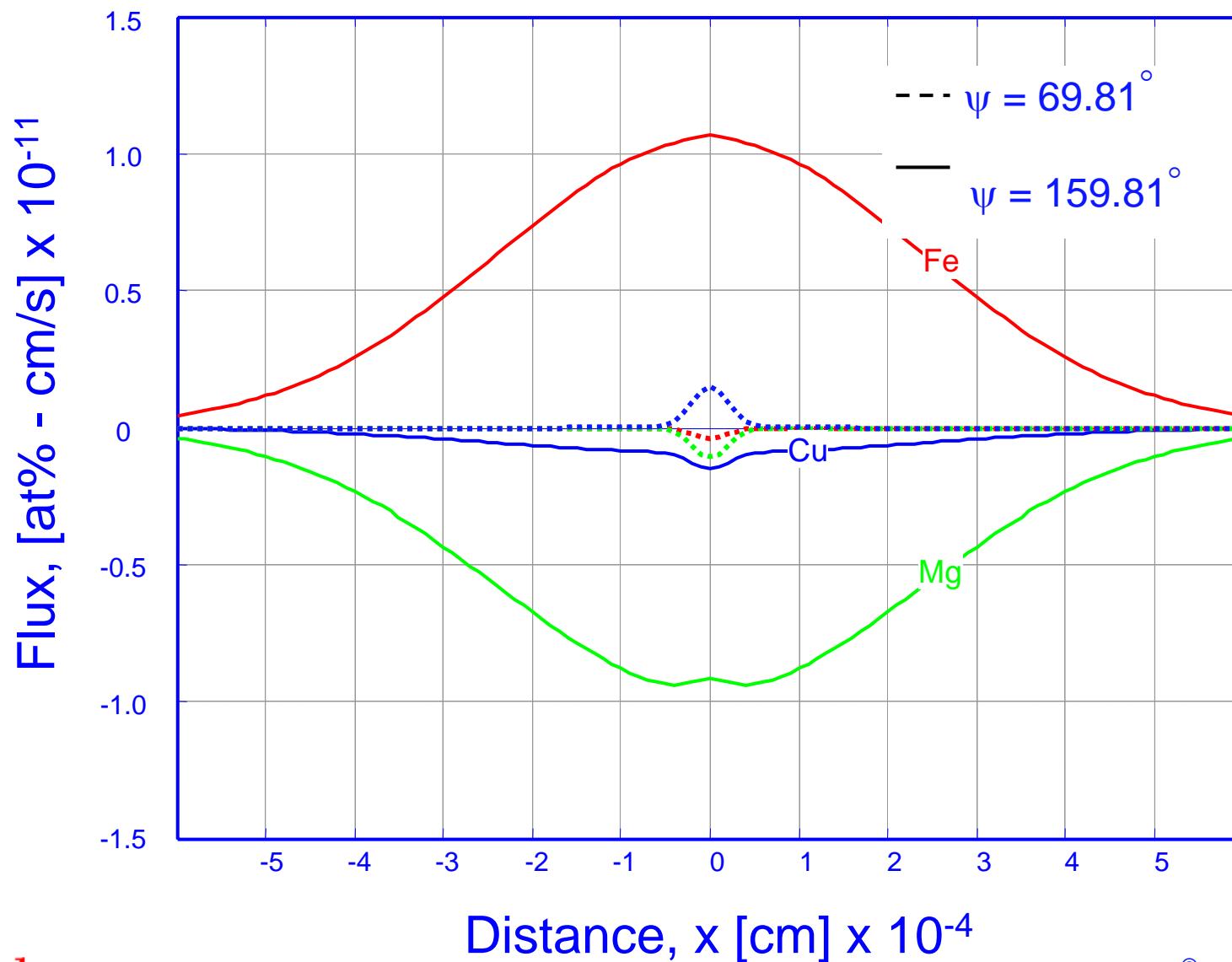
# Fe–32.39, Mg–49.41, Ca–18.20 [at%]



# Flux versus Distance



# Flux versus Distance



Composition [at%]	$\psi^*$ deg	Minimum M Euler Angle	Minimum Abs. Flux Euler Angle	Stationary ZFP Euler Angle
Cr – 10 Al – 10 Ni – 80	≈ -29 ≈ 151	≈ 145	≈ 140	≈ -38.1 ≈ 141.9 (Ni)
Ni – 42 Al – 39 Fe – 19	≈ 45 ≈ 225	≈ 52	≈ 62	≈ 64.31 ≈ 244.31 (Ni)
Ni – 43.50 Zn – 25.00 Cu – 31.50	≈ -9.7 ≈ 170.3	≈ 172	≈ 175	≈ -3.64 ≈ 176.36 (Zn)
Fe – 32.39 Mg – 49.41 Ca – 18.20	≈ 69.8 ≈ 249.8	≈ 72	≈ 65	≈ 71.94 ≈ 251.94 (Fe)



# Summary

- A new MatLab code was developed at RPI to simulate multicomponent diffusion in single-phase ternary alloy systems.
- Numerical data obtained using MatLab script was compared with the output provided by *Profiler* (DOS), and *Kaleidagraph*© (Mac-OS).
- The new code was tested with a few alloy sytems including the ternary alloy, 43.5 at%-Ni, 25 at%-Zn, 31.5 at%-Cu, where diffusive spreading is reduced for couples located in composition space close to the minor eigenvalues located at  $\psi^* = -9.65^\circ$  and  $\psi^* = 170.34^\circ$ .
- Stationary ZFPs of the minor component occur at  $\psi_{\text{ZFP}}^{\text{Zn}} = -3.64^\circ$  and also  $\psi_{\text{ZFP}}^{\text{Zn}} = 176.36^\circ$ .
- We predict the end-member compositions for which minimum mass transport rate,  $M$ , occurs and for different systems.
- Code development work remains in progress.

